



# Sound of Music

## How It Works

Session 2

Resonance: Building Musical Sounds

OLLI at Illinois

Spring 2020

D. H. Tracy



The Most Unusual Musical Instruments of the World  
*PerdoscopeTV (YouTube 2016)*



# An Ear for Music

## Session 2 Resonance and Building Complex Sounds

OLLI at Illinois  
Spring 2024

D. H. Tracy

# Course Outline



1. Building Blocks: Some basic concepts
- 2. Resonance: Building Complex Sounds**
3. Hearing and the Ear
4. Musical Scales and Musical Notation
5. Musical Instruments: Strings and Others
6. Musical Instruments: Pipes
7. Human Voice and Singing
8. Harmony and Dissonance; Chords

# Question Times

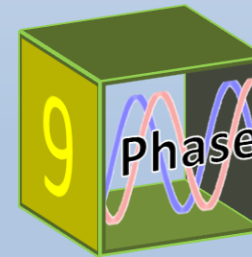
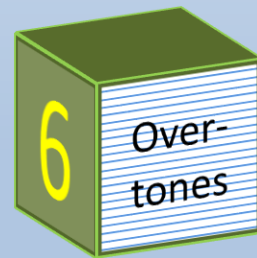
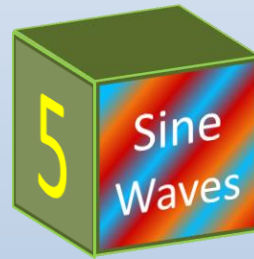


- Zoomland
- In Person

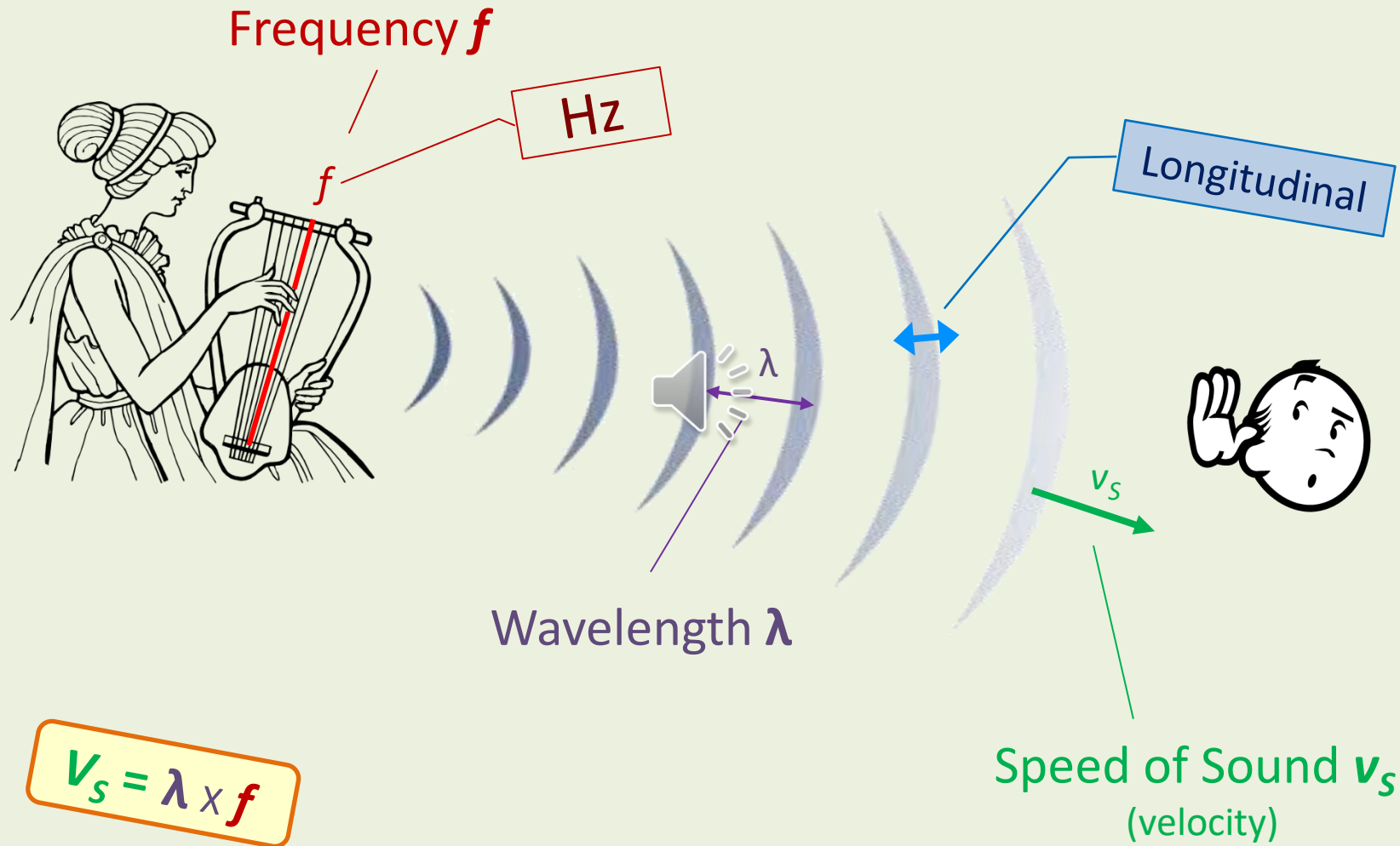
- Halfway Through
- At the End



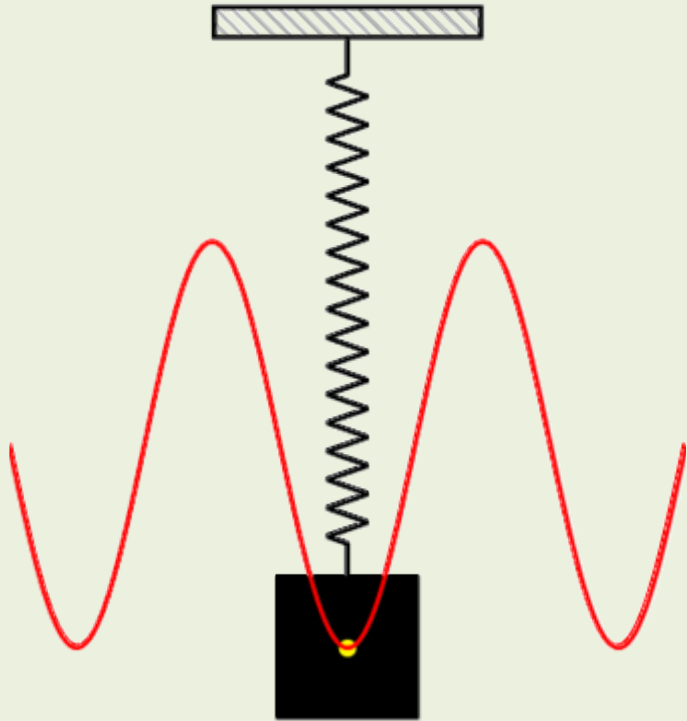
# Session 1 Outline: Building Blocks



# Sound As Compression Waves



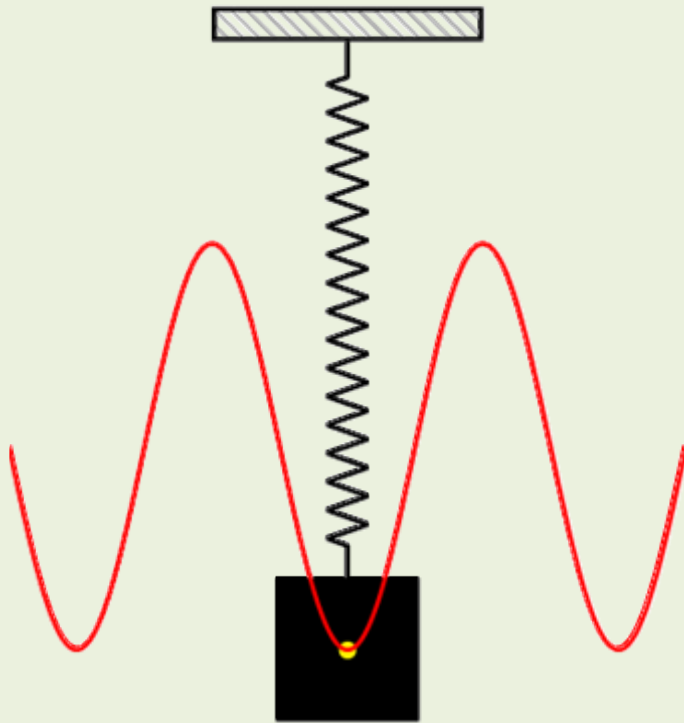
# Simple Harmonic Oscillator



Imgur.com



# Simple Harmonic Oscillator



Imgur.com

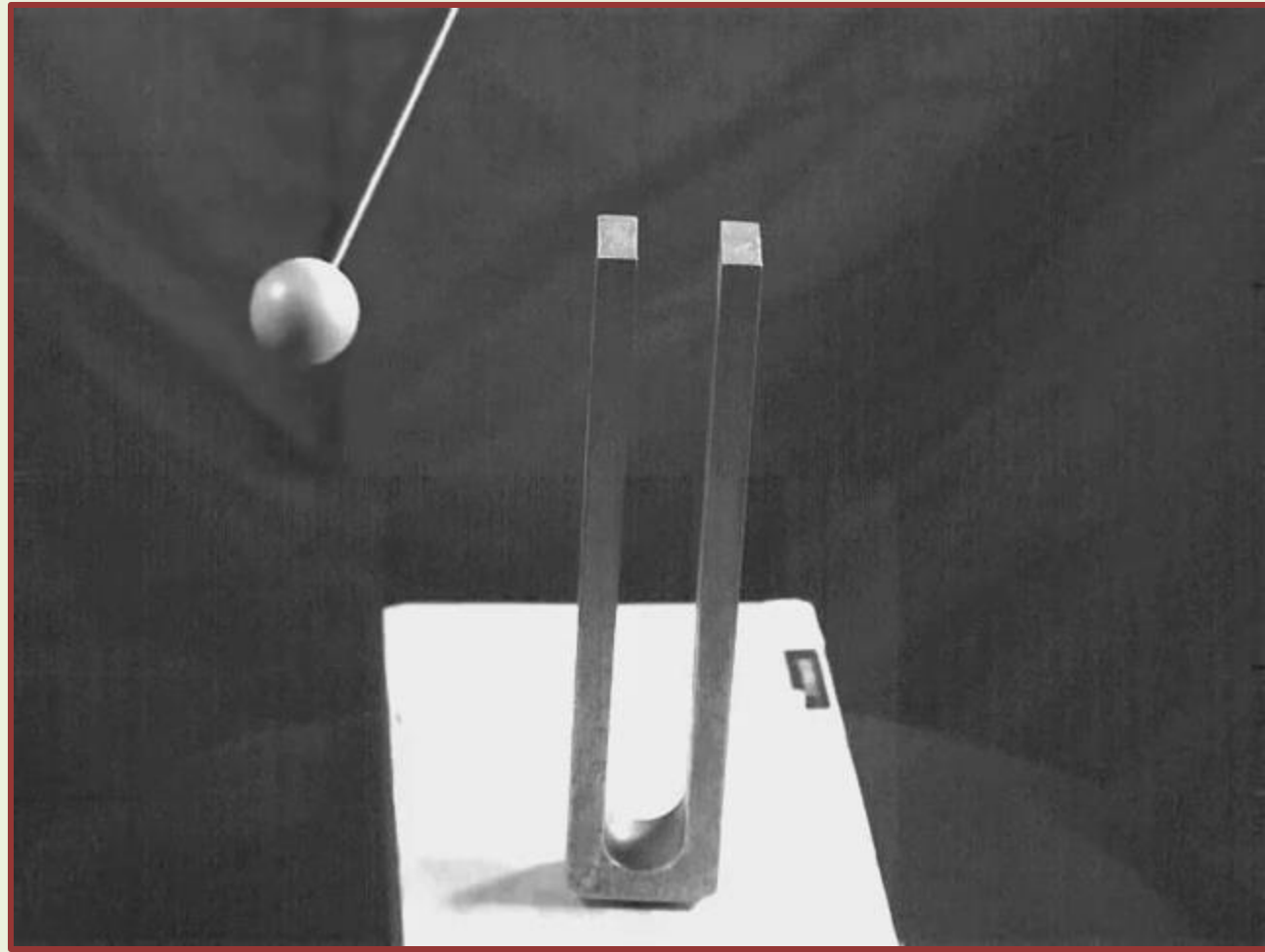


James Dodd: You-Tube





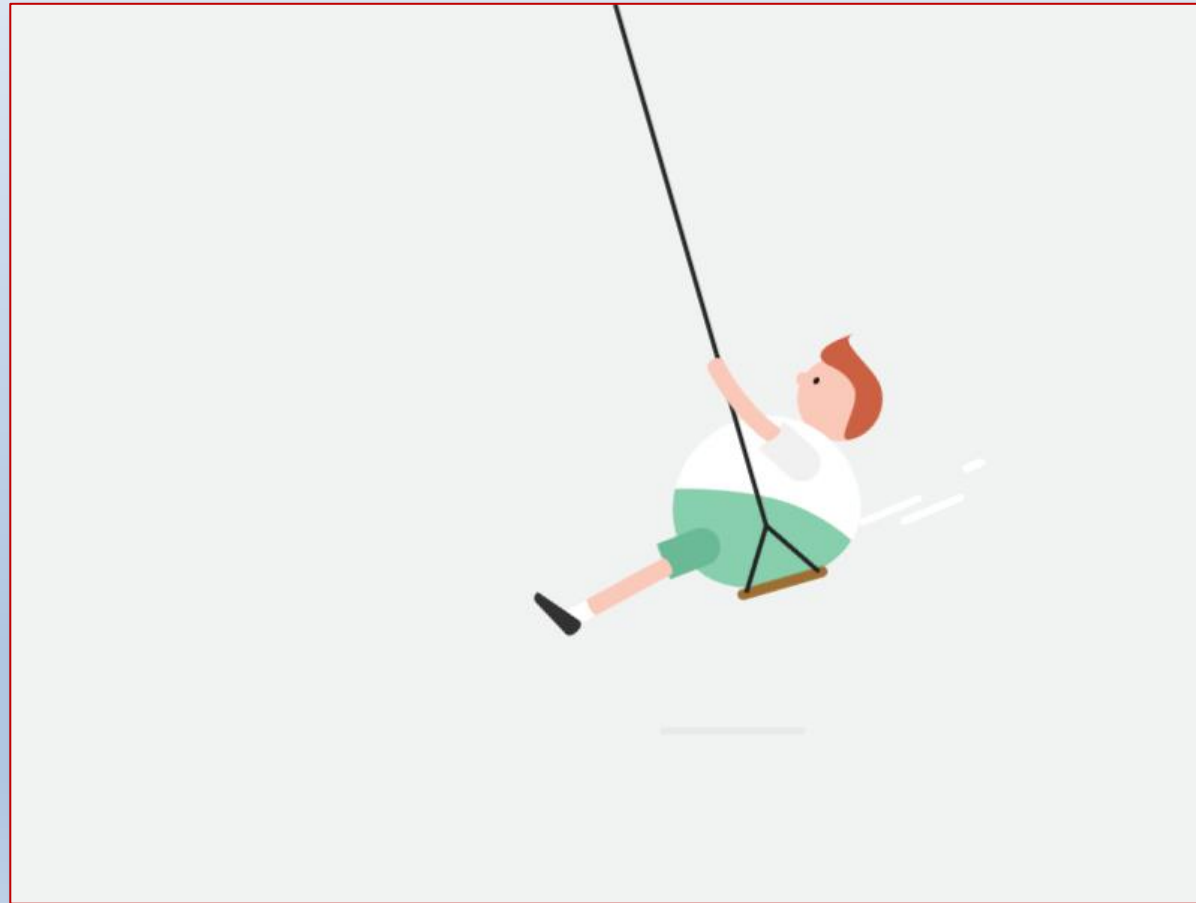
# Tuning Fork



Michigan Tech  
YouTube  
9/11/2014



# Resonators can be excited by well-timed nudges

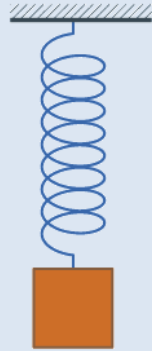


# How can we make Sine Waves?

- Simple Harmonic Oscillators do it



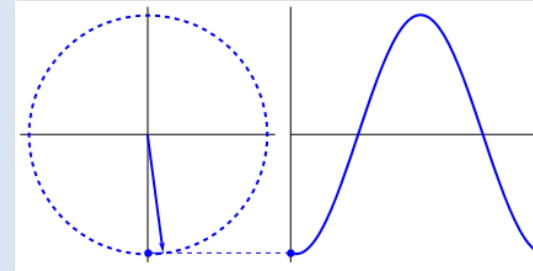
Simple  
Pendulum



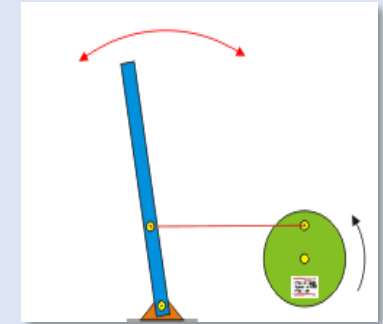
Mass on  
Spring



*e.g.*  
Tuning Fork



Circular  
Projection

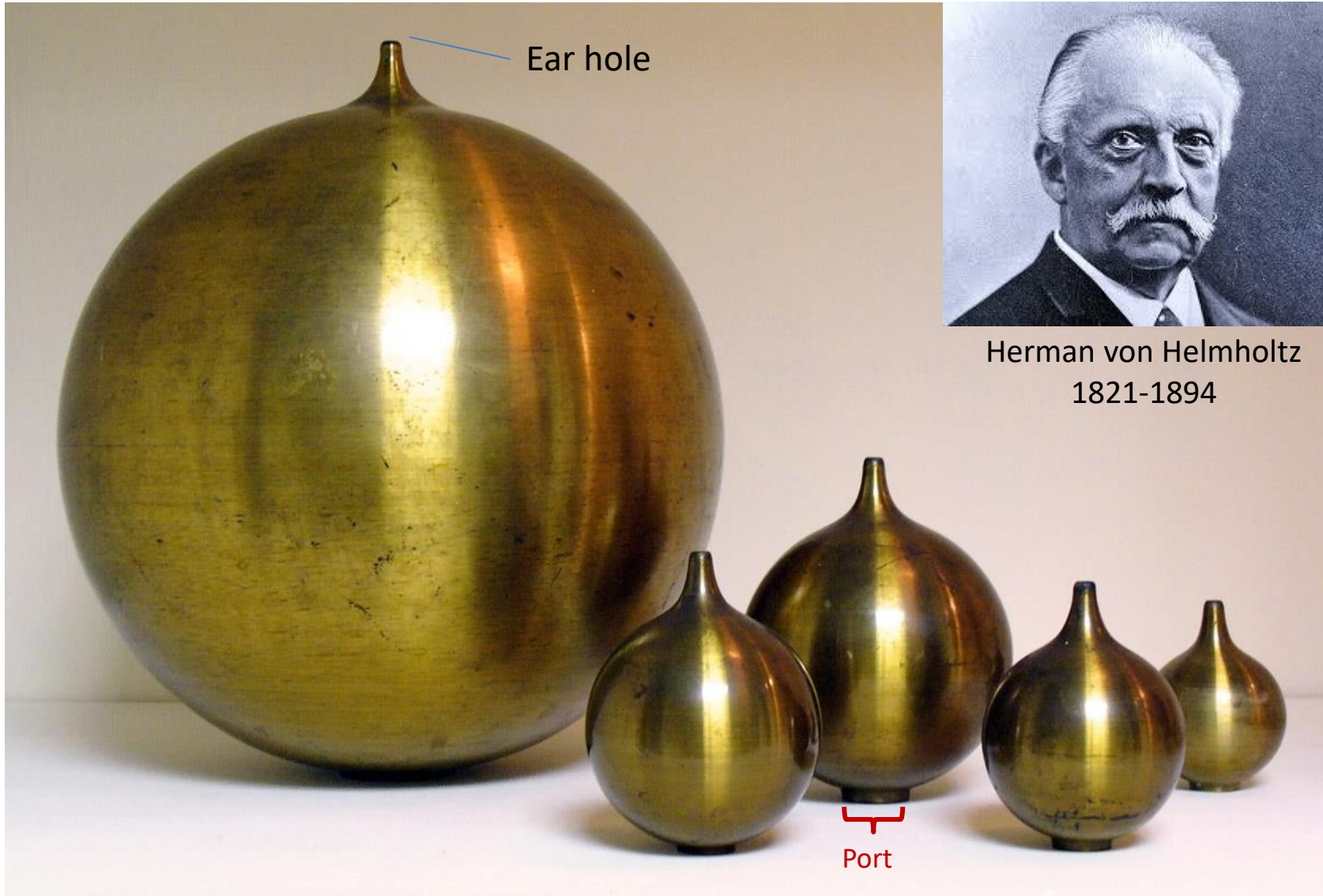


*e.g.* Rotational  
Crank Mechanism

- Electronics can also do it



# Helmholtz Resonators

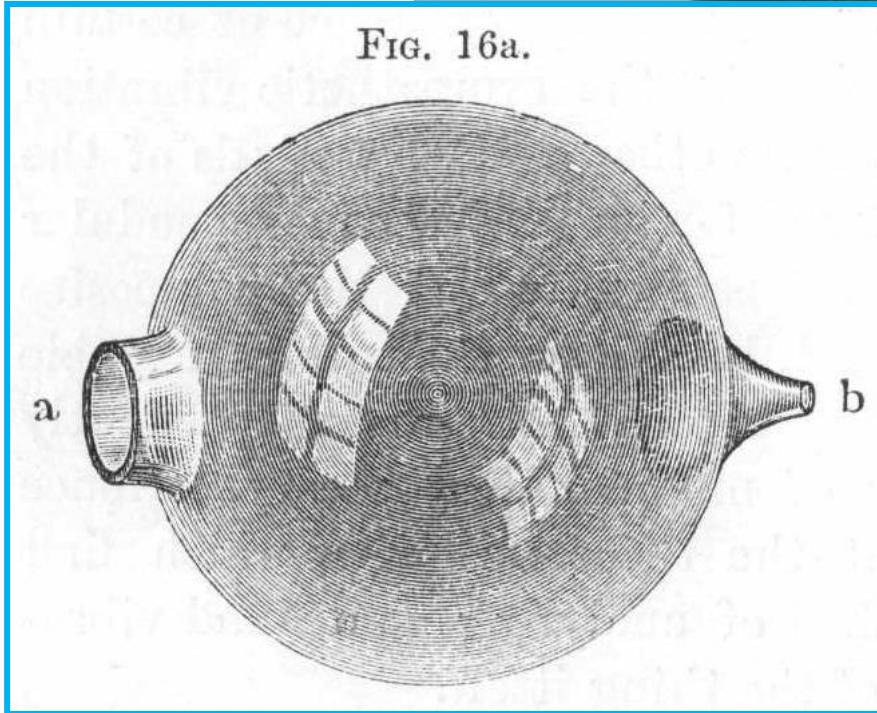
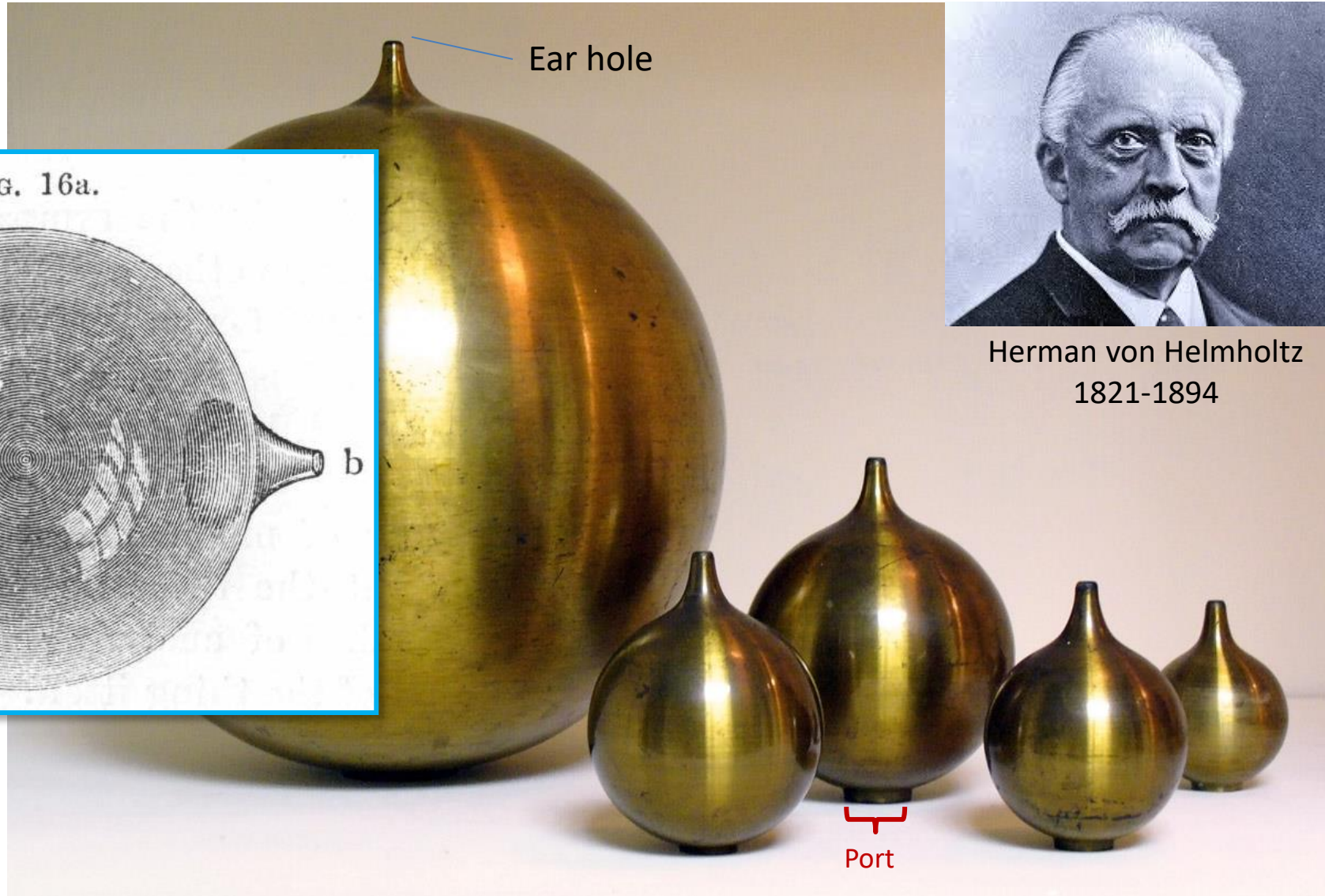




# Helmholtz Resonators



Herman von Helmholtz  
1821-1894



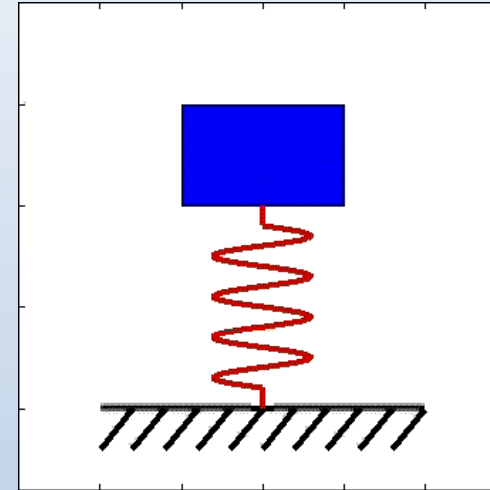
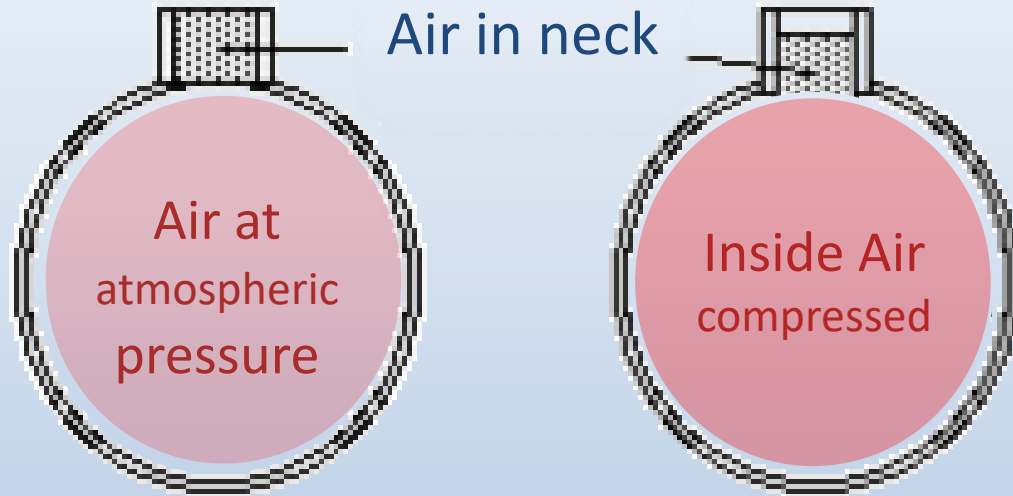


Smithsonian National Museum of  
American History (2012)

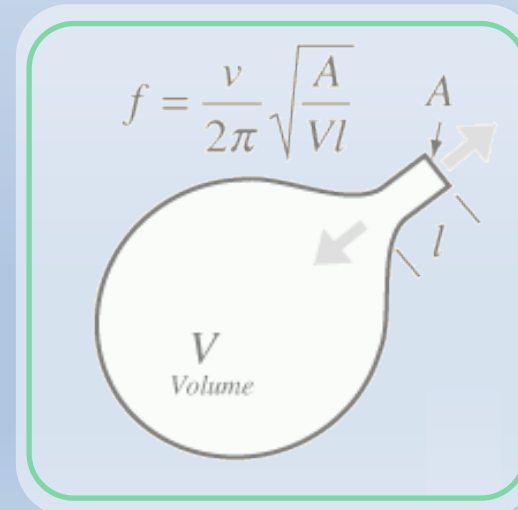


# Helmholtz Resonators

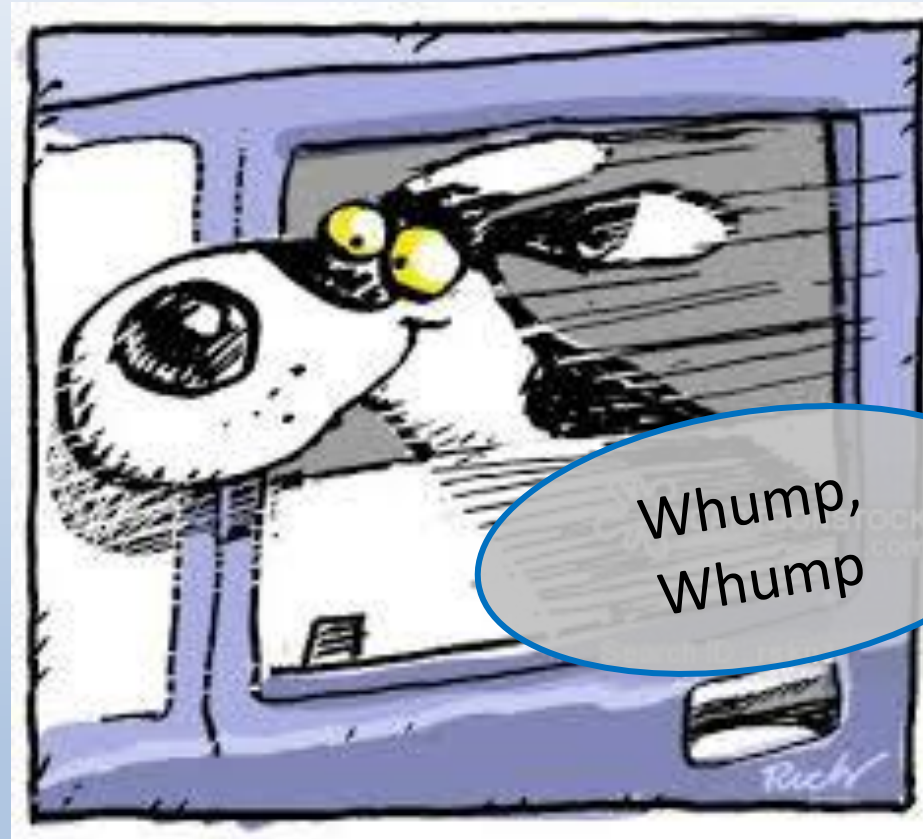
Simple Harmonic Oscillator



- The air in the Neck is the Mass
- The air in the volume acts as the spring



Ever experience a Whump-Whump in your car when a rear window is cracked open?

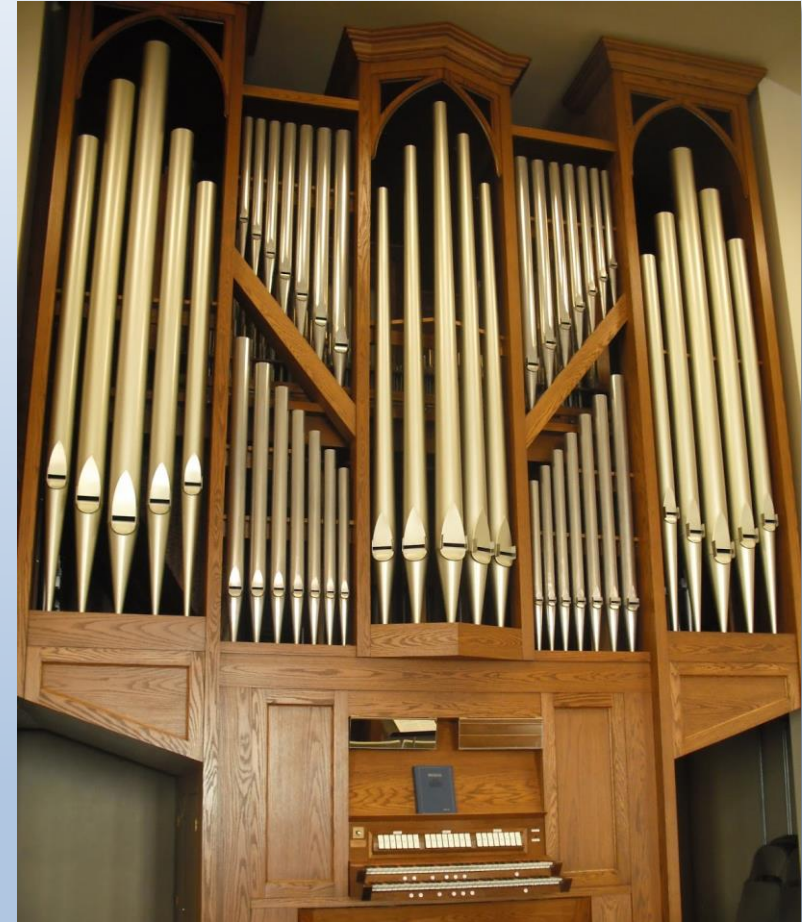




Ever experience a Whump-Whump in your car when a rear window is cracked open?



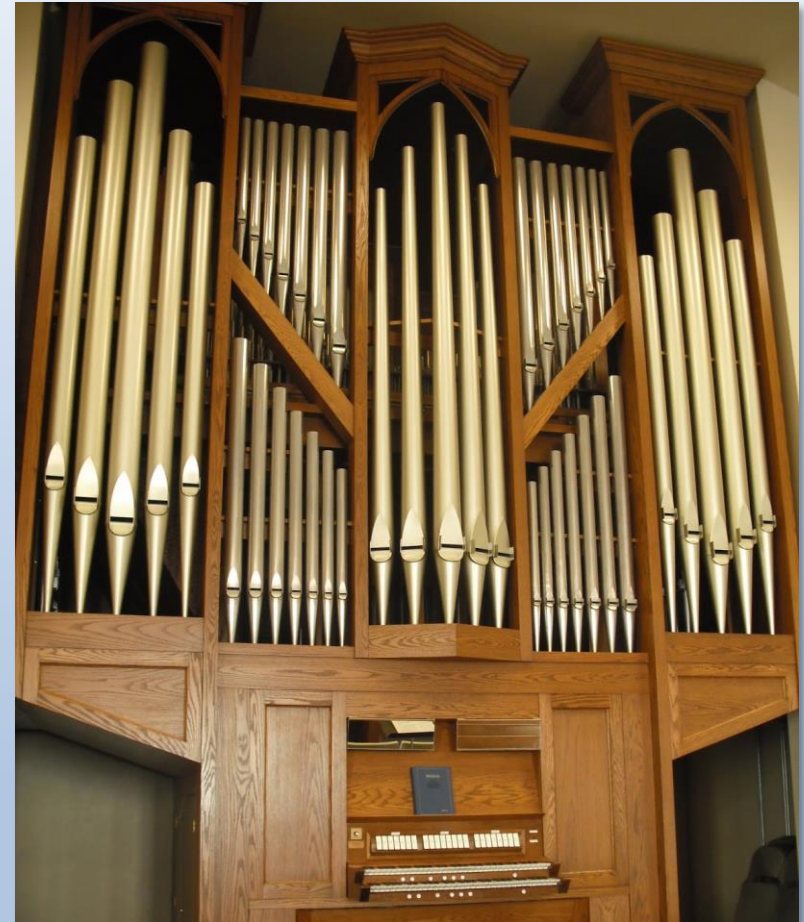
# Resonators Using Strings and Pipes



# Resonators Using Strings and Pipes



Anne Sullivan playing *Siciliana* (Respighi)





# Resonators Using Strings and Pipes



Prelude in C Major (Bach): Brian of the LDS [ [Liahona.net](http://Liahona.net) ]



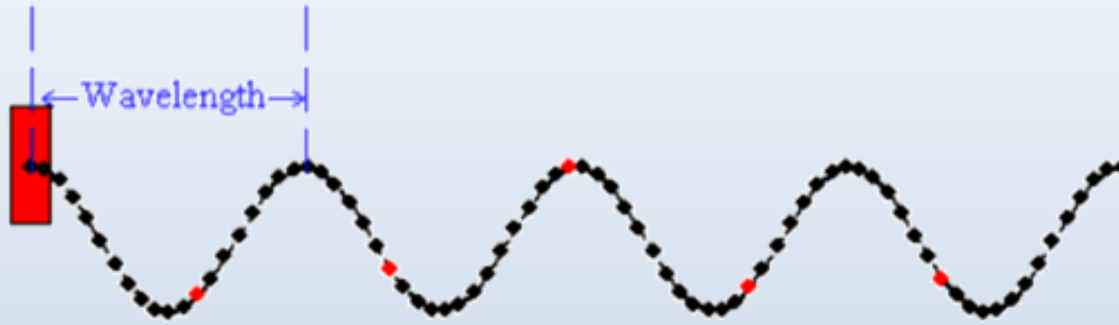
# Resonators Using Strings and Pipes



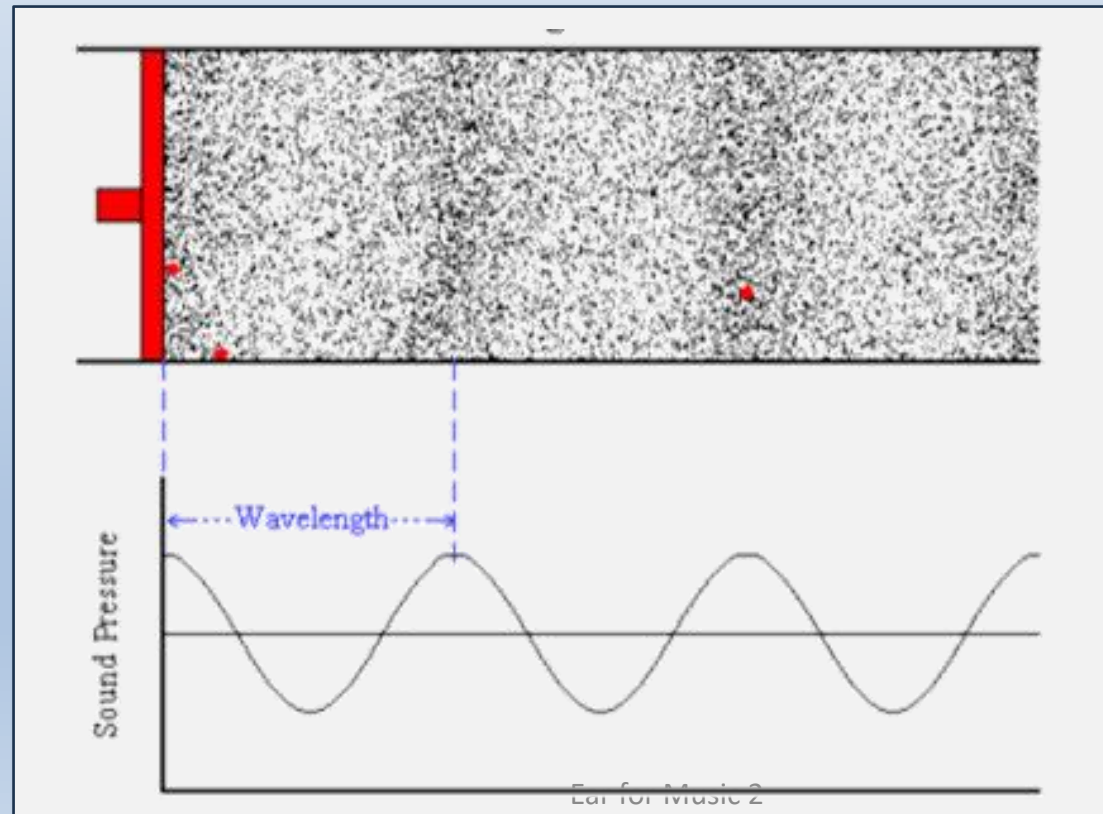
Easiest way to understand these is via the concept of “Standing Waves”



# Traveling Waves



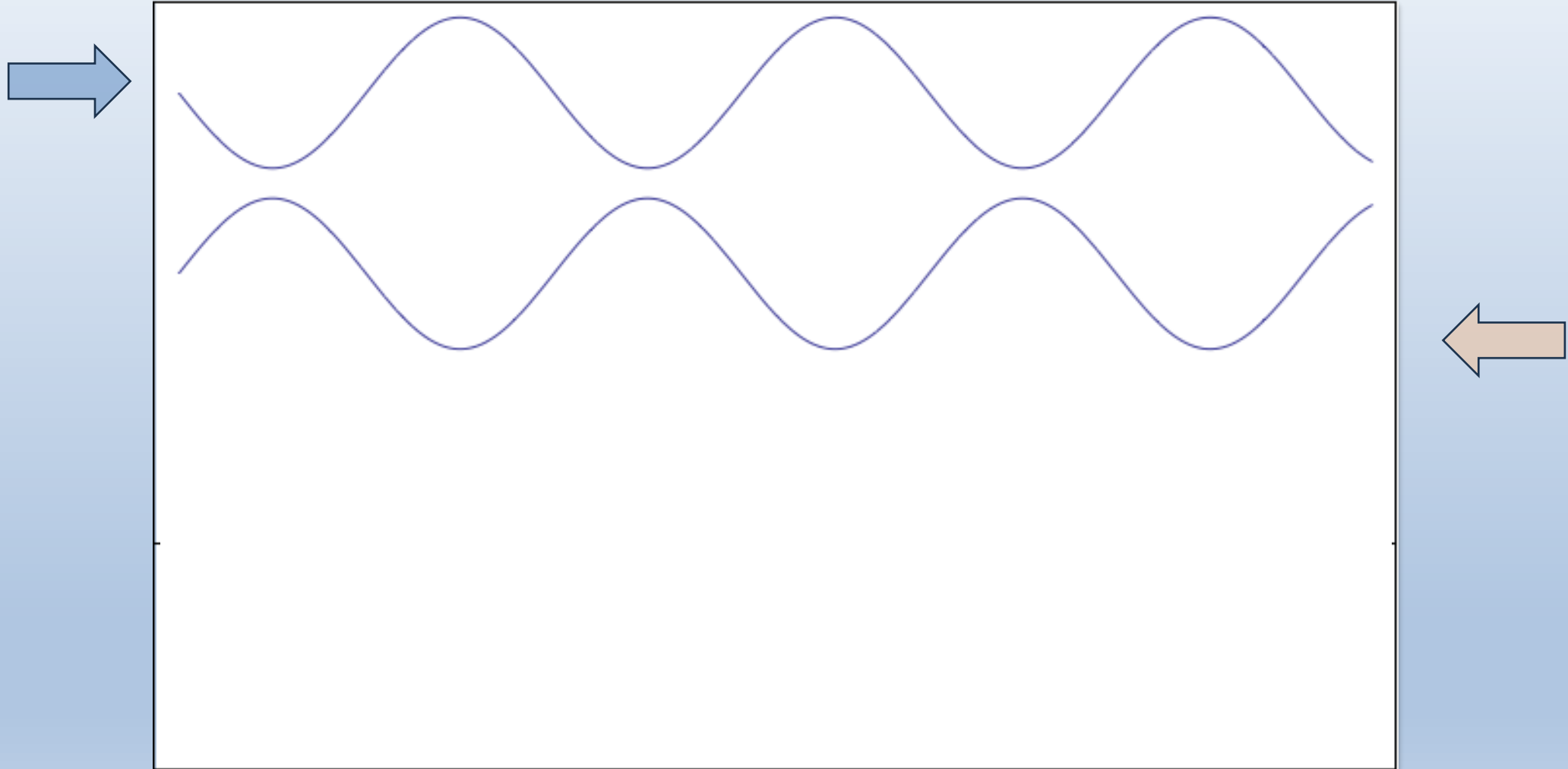
Transverse Waves  
on a Rope or String



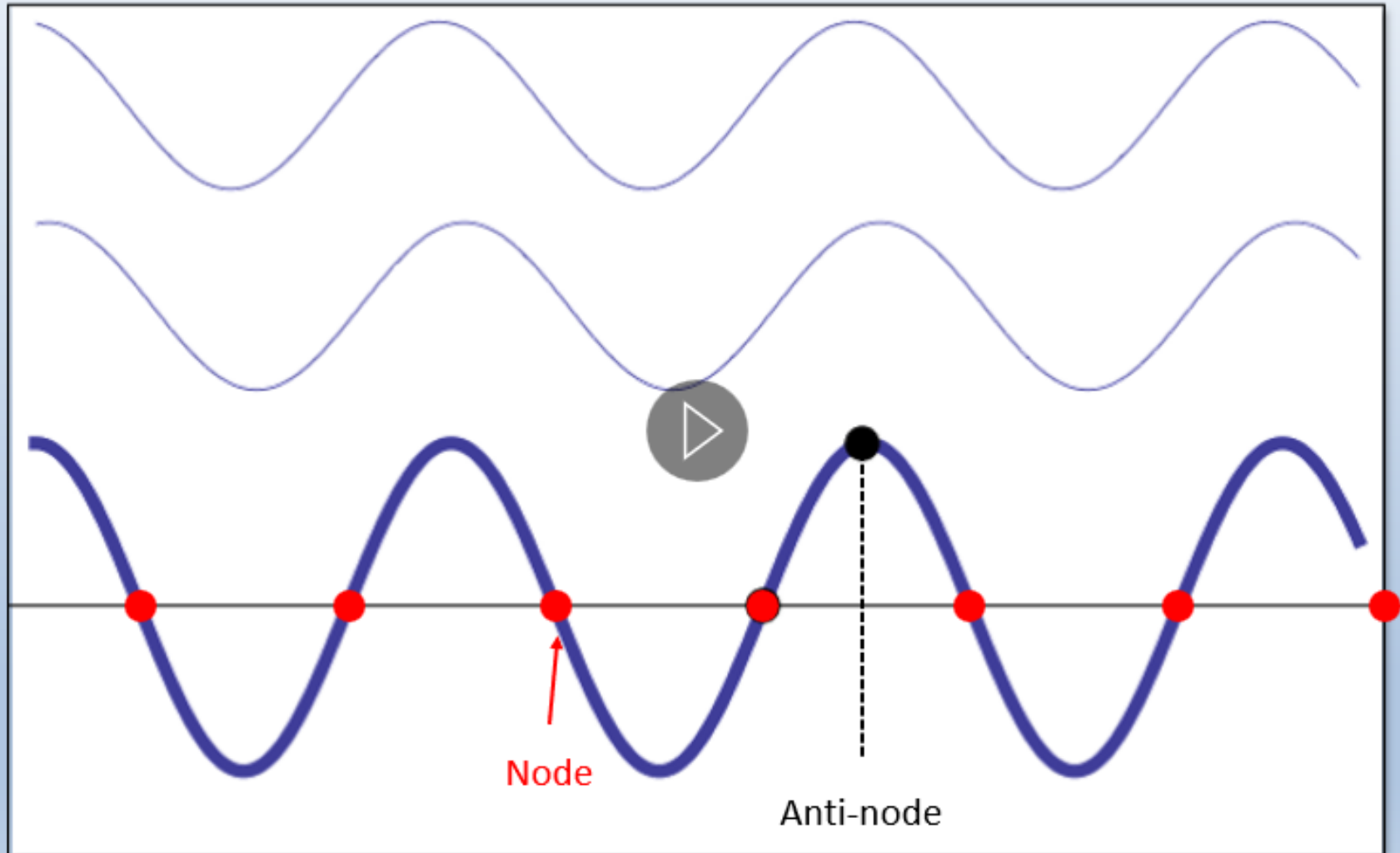
Longitudinal  
Sound Waves



## 2 Traveling Waves Combine... To Form a **Standing Wave**

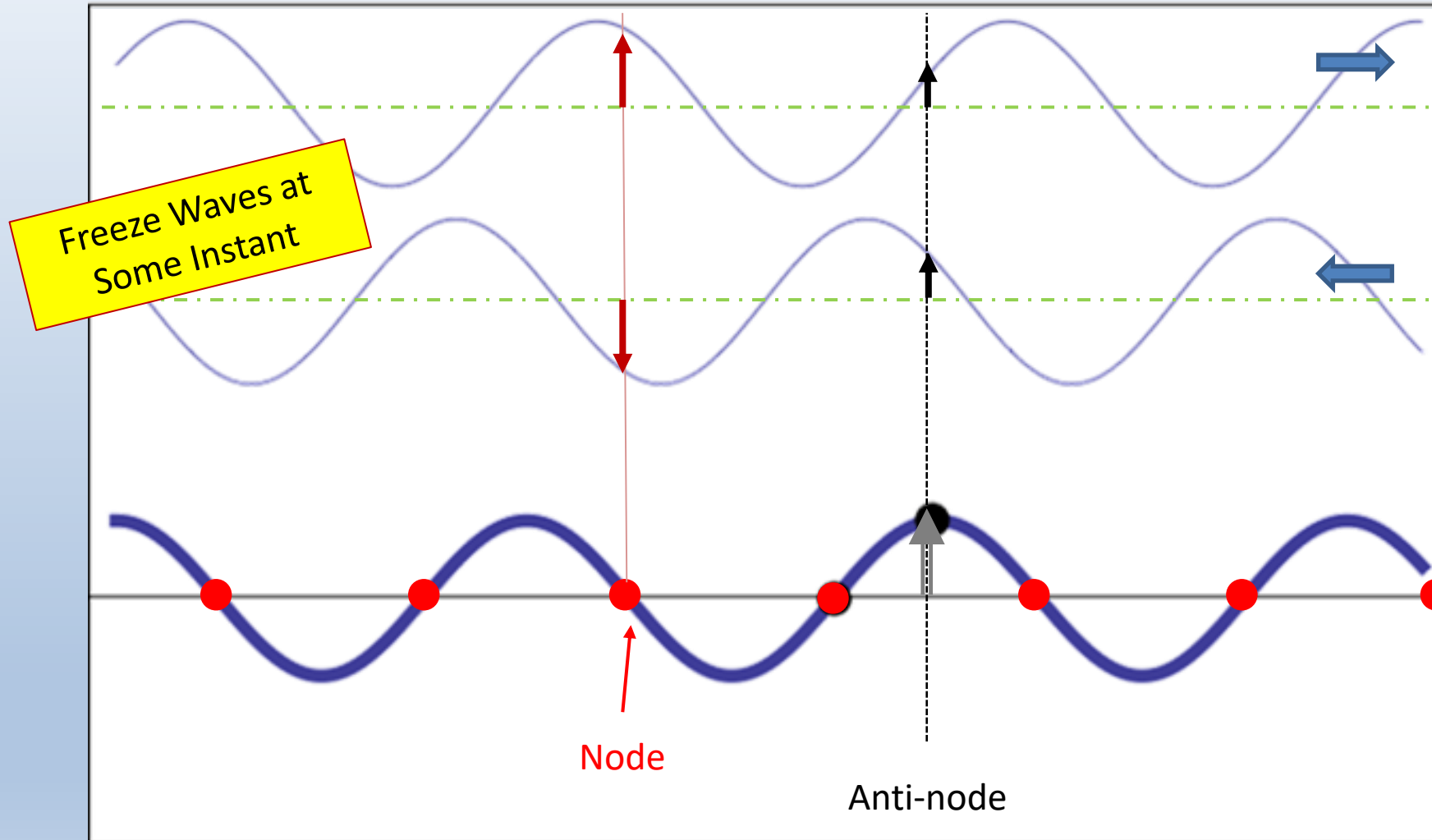


## 2 Traveling Waves Combine... To Form a **Standing Wave**





## 2 Traveling Waves Combine... To Form a Standing Wave



# Standing Waves in Air

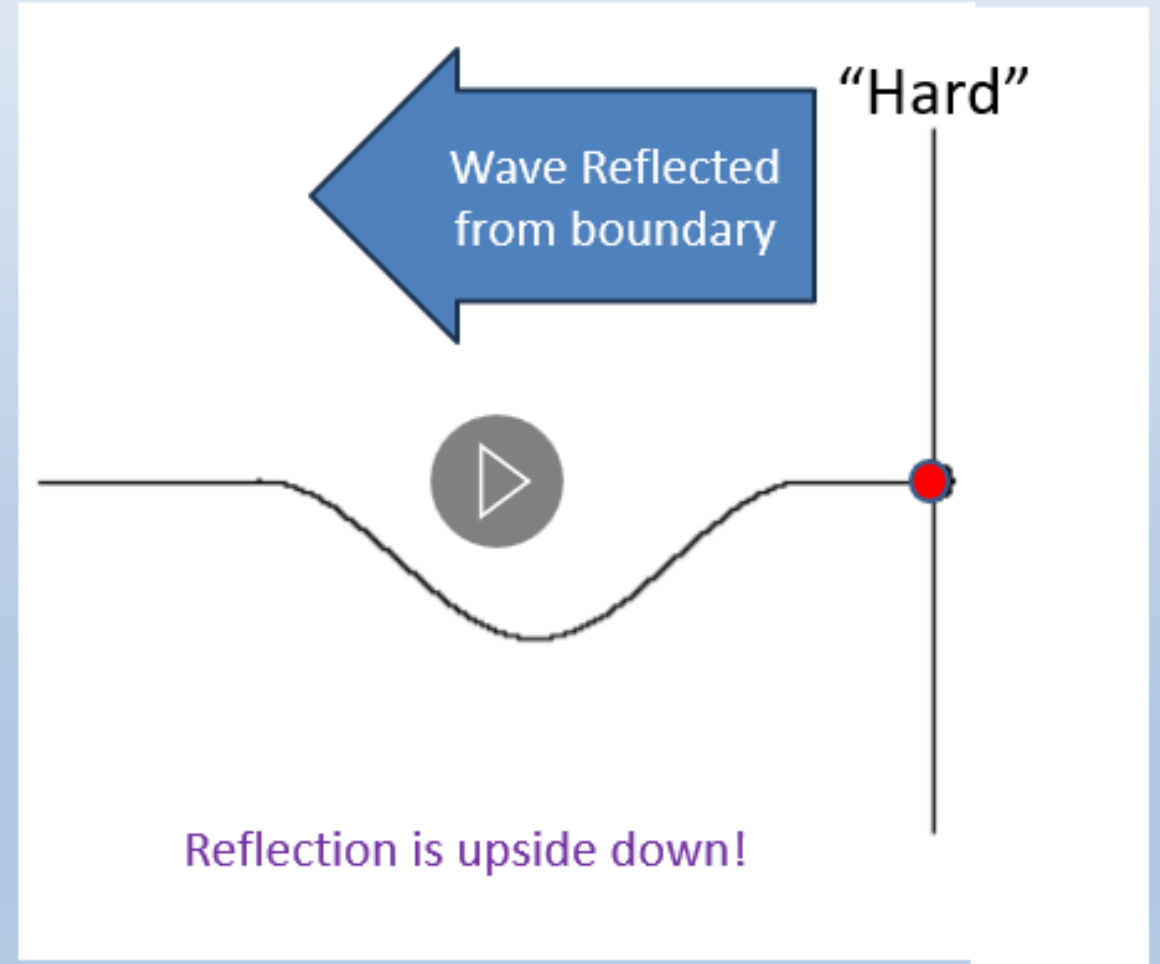
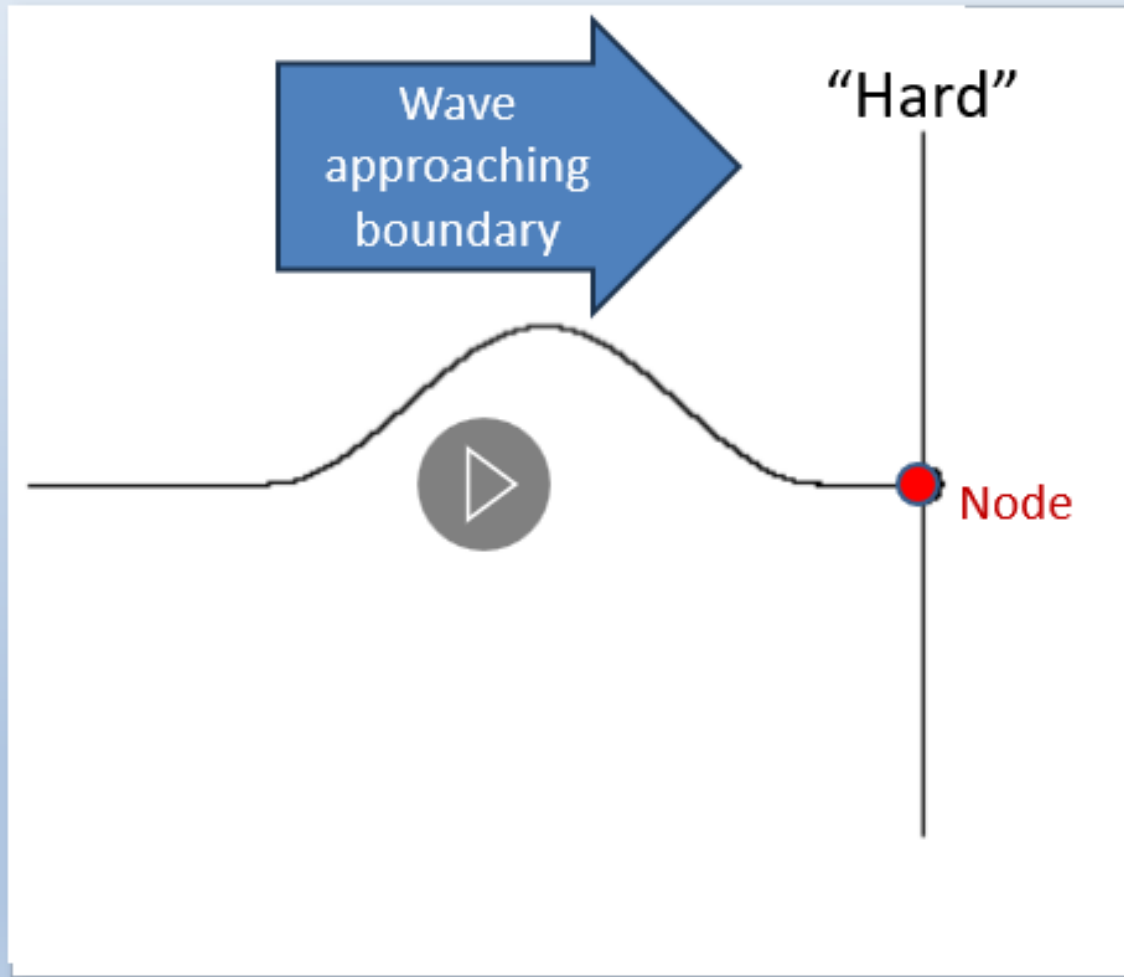


A Demo We could do  
(but didn't)



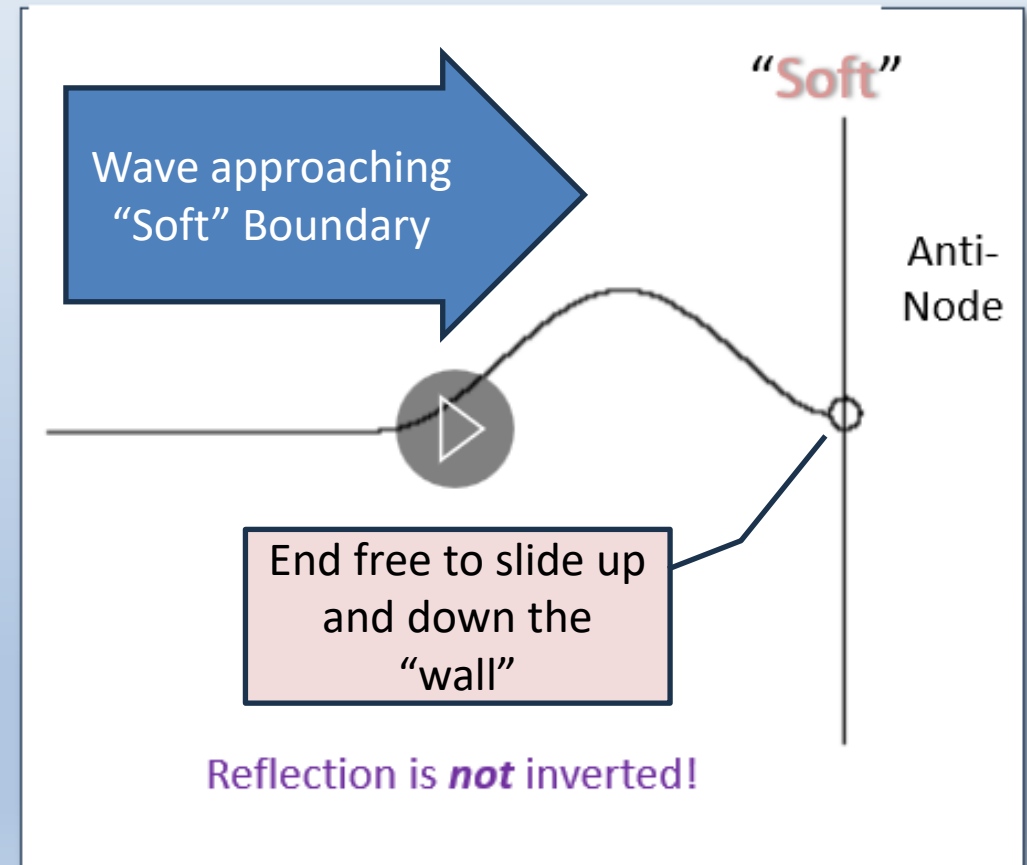
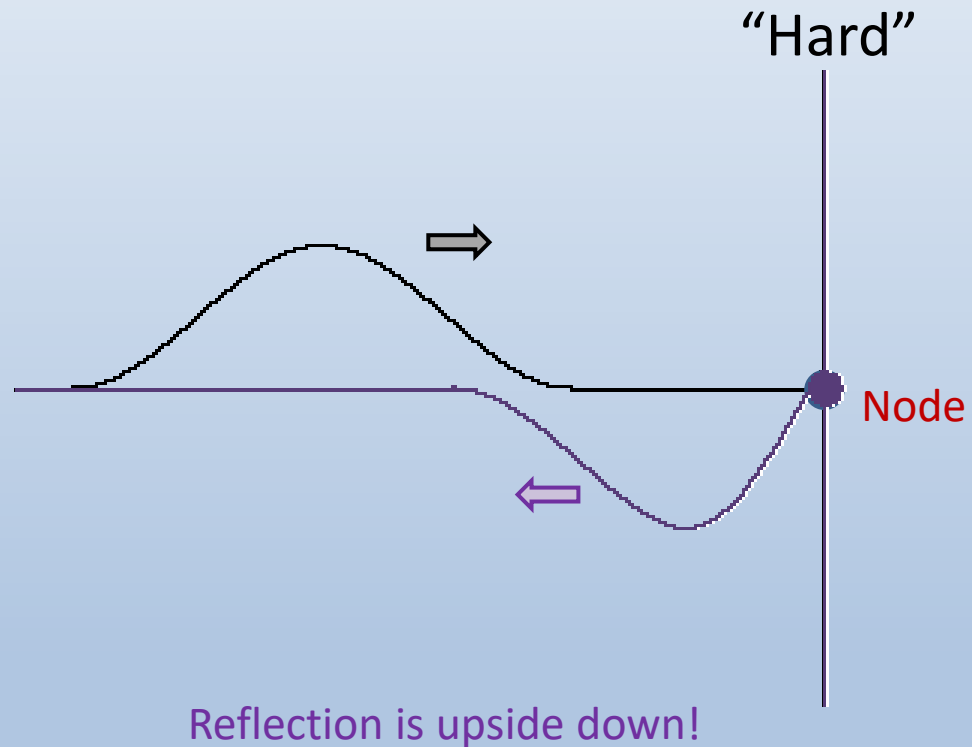
# Q: How Do We Make Standing Waves?

## A: Reflections at a Boundary



# Q: How Do We Make Standing Waves?

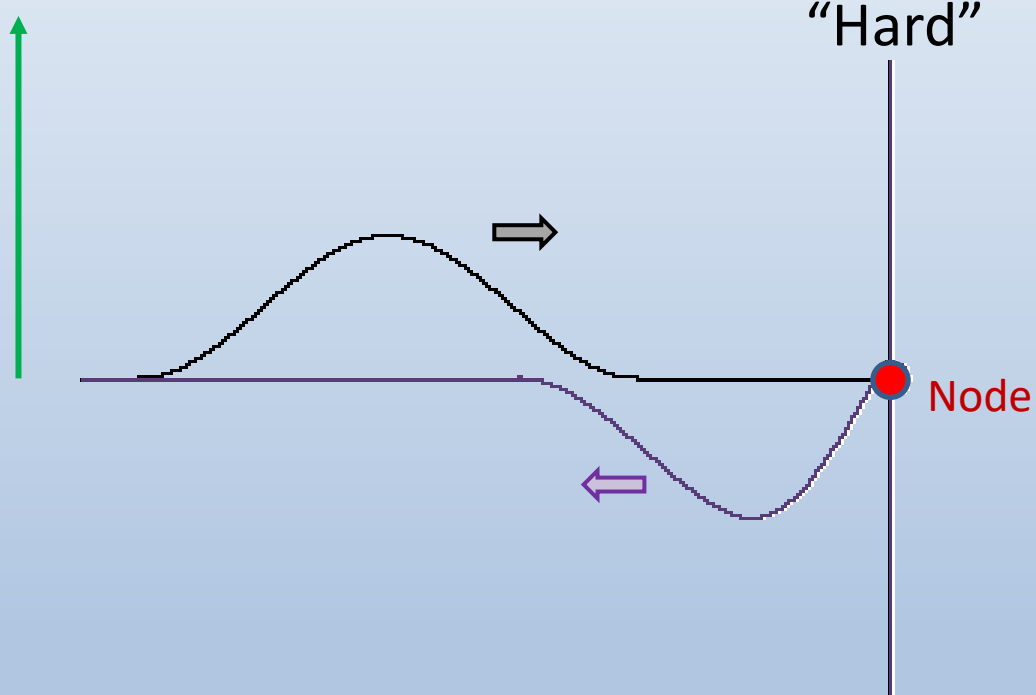
## A: Reflections at a Boundary



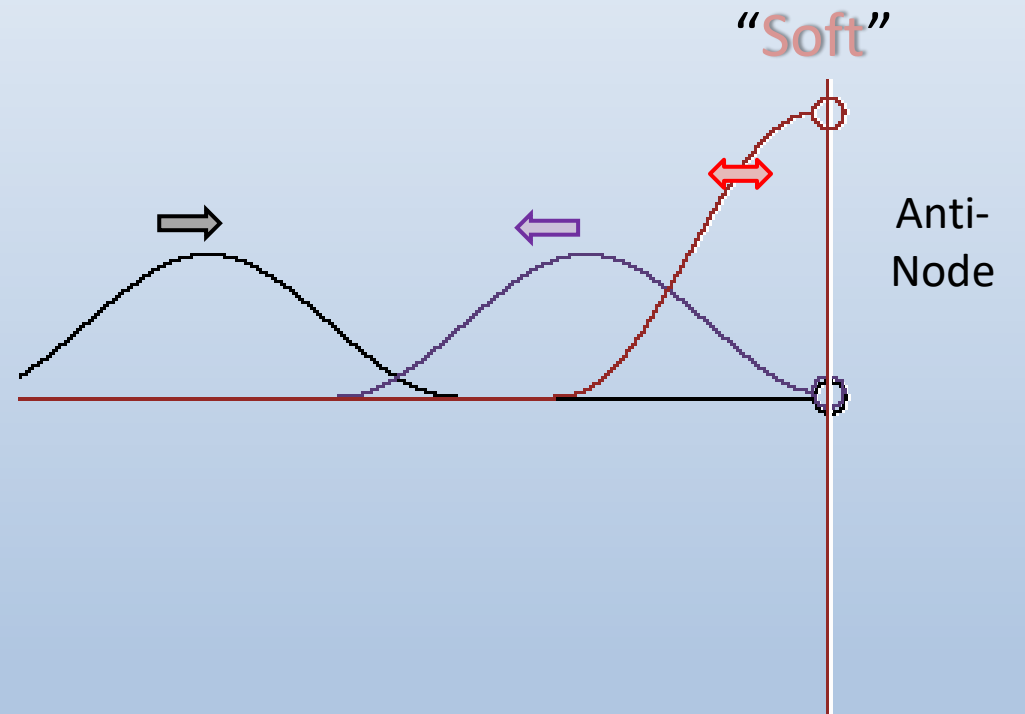
# Q: How Do We Make Standing Waves?

## A: Reflections at a Boundary

Displacement



Reflection is upside down!



Reflection is *not* inverted!

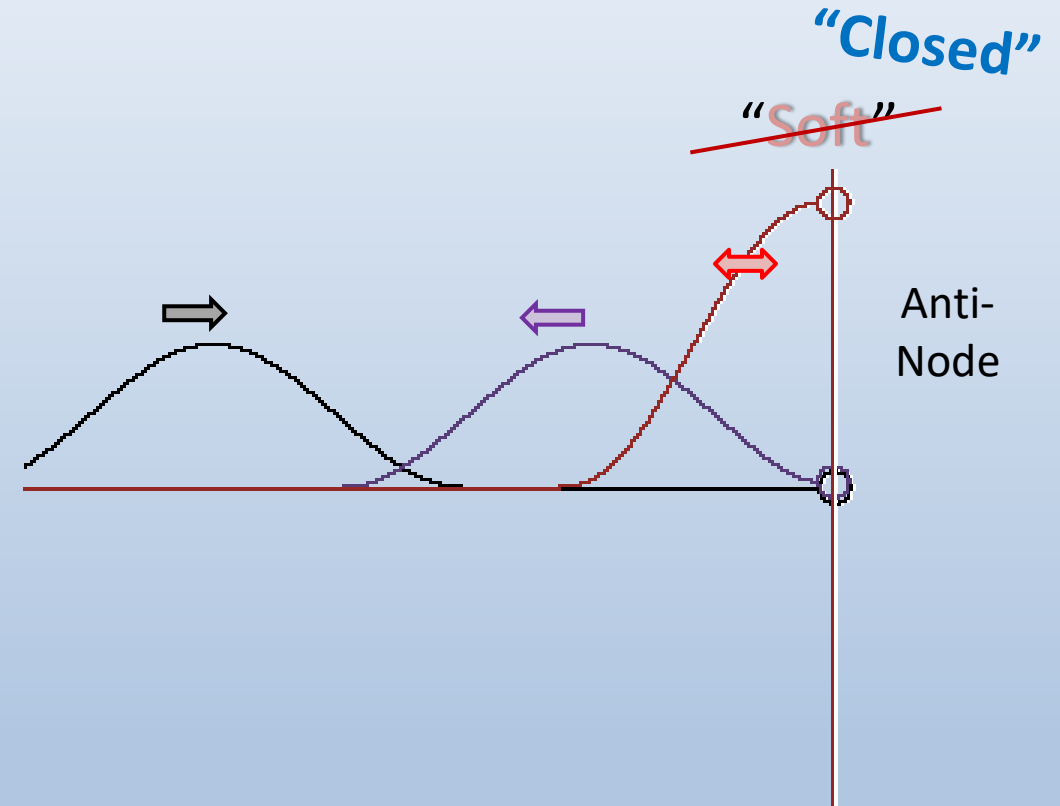
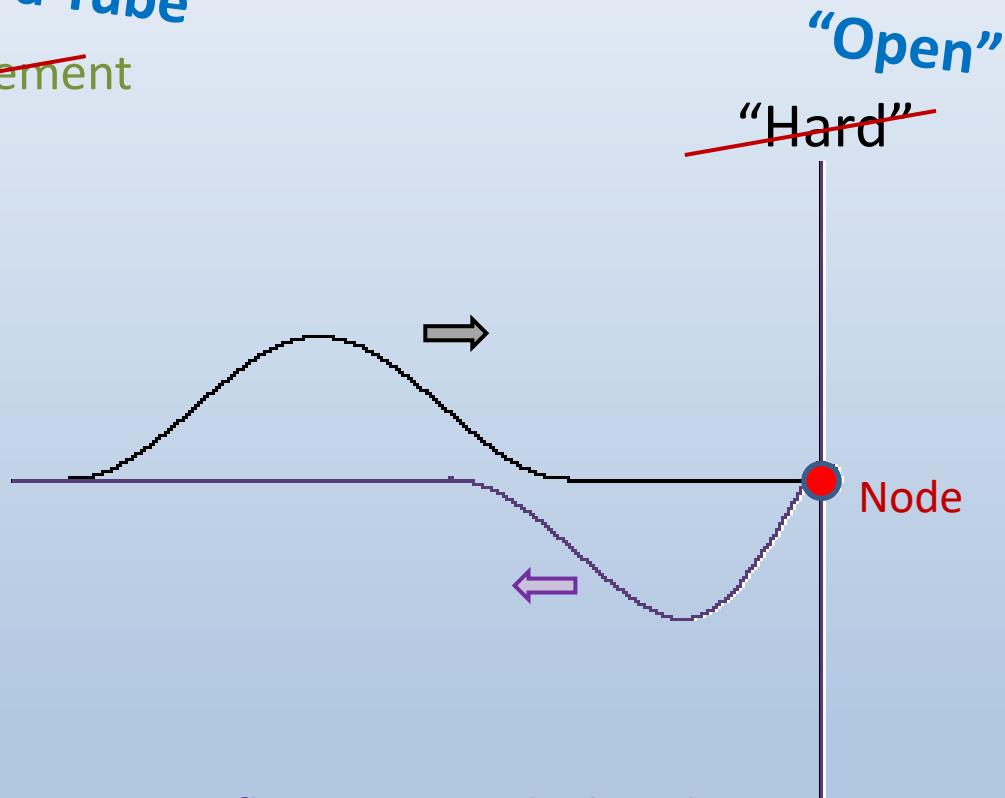


# Q: How Do We Make Standing Waves?

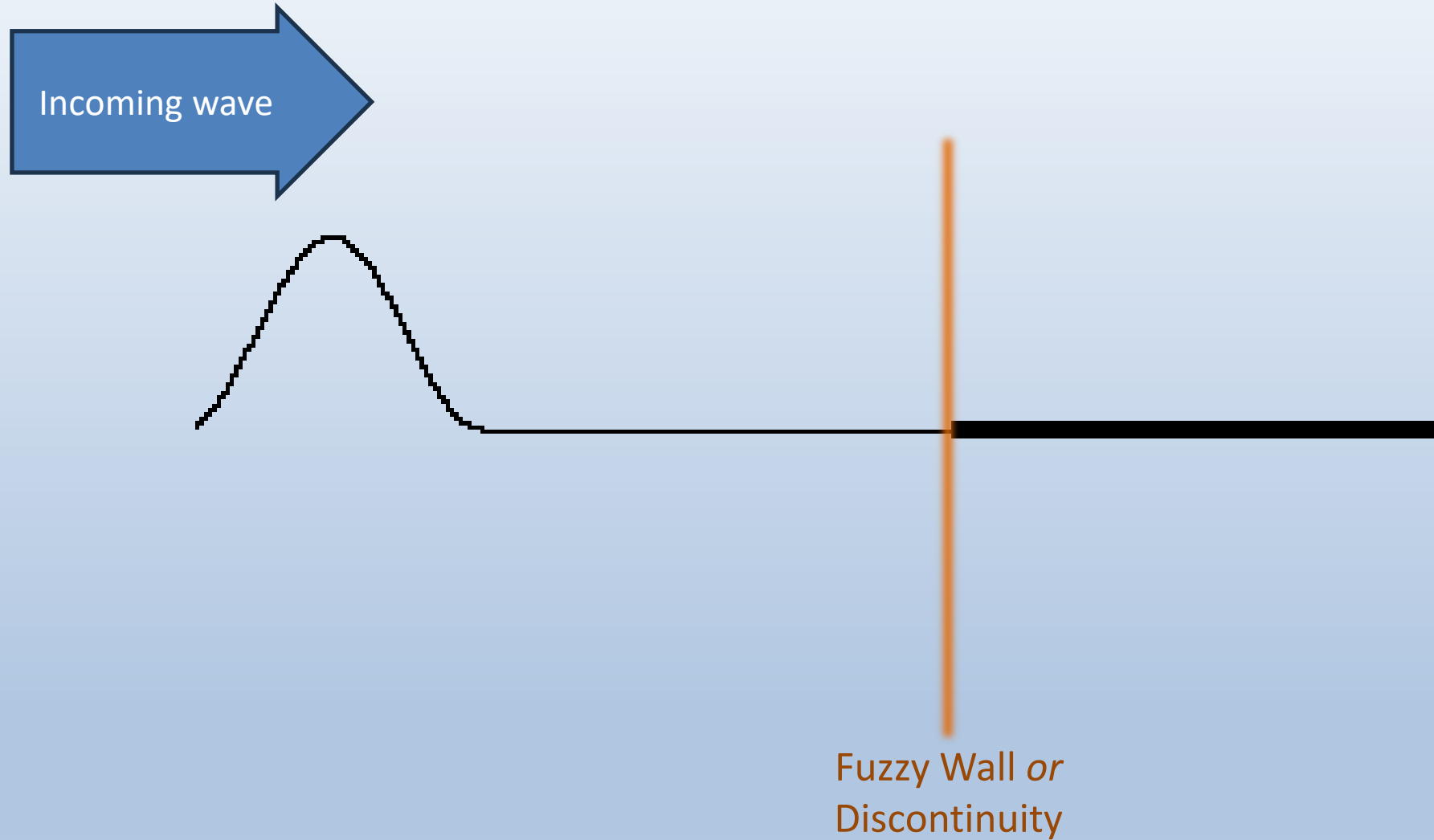
## A: Reflections at a Boundary

Air Pressure  
in a Tube

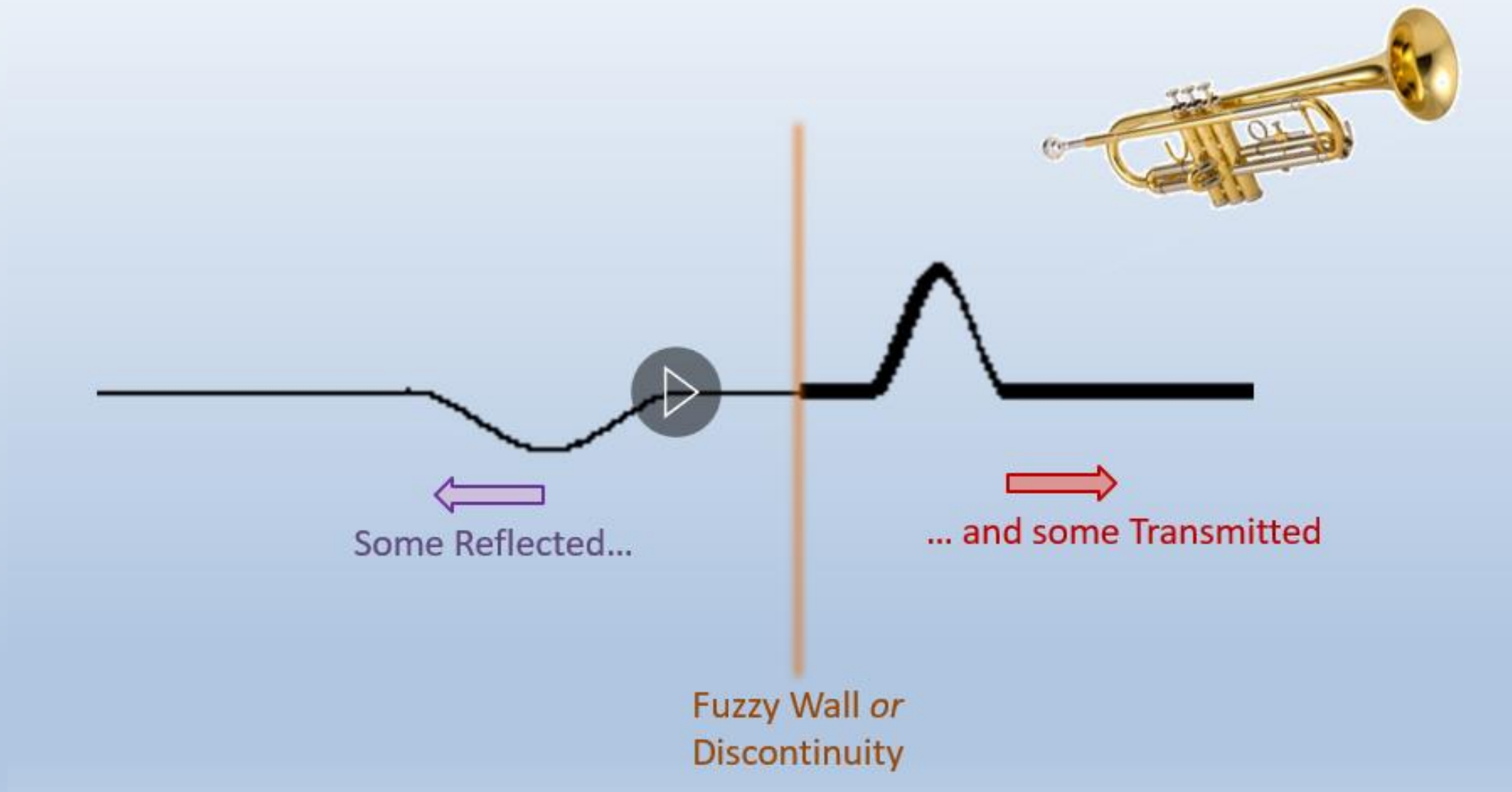
~~Displacement~~



# Partial Reflection



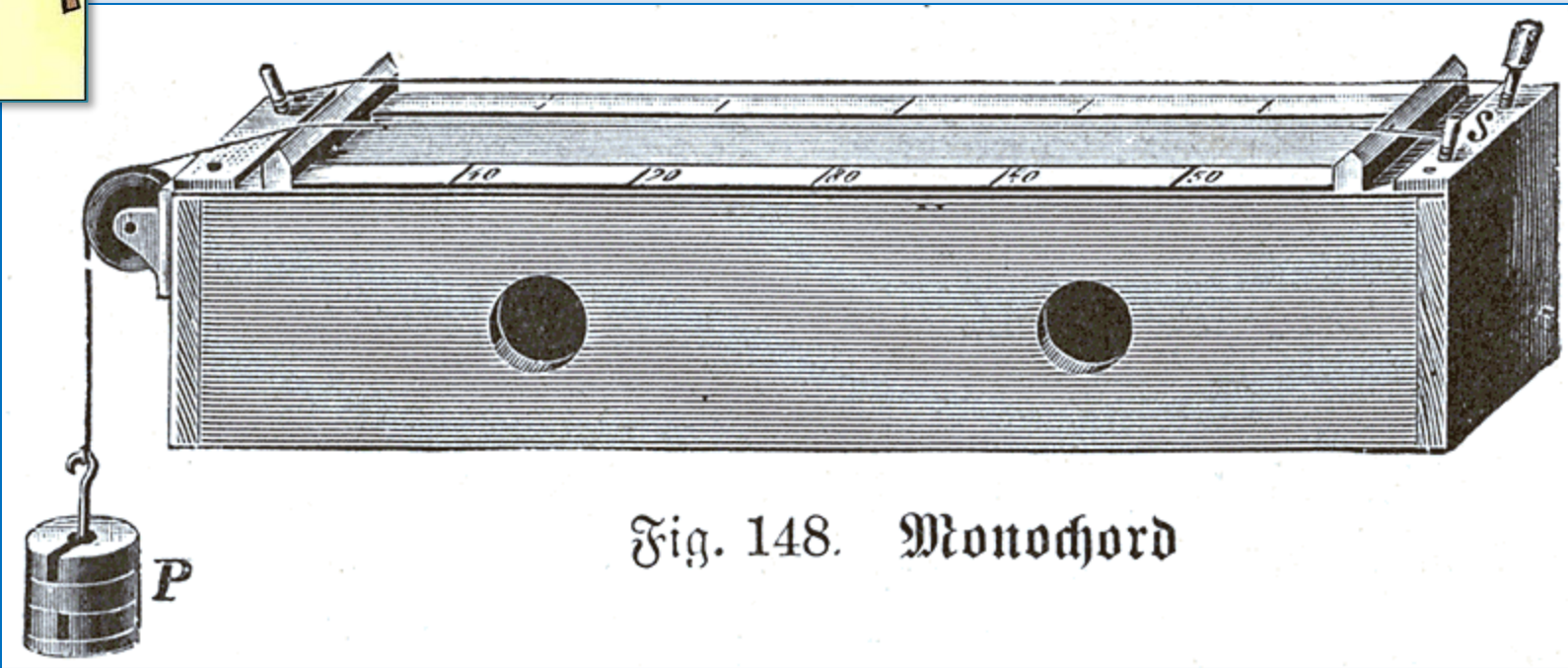
# Partial Reflection





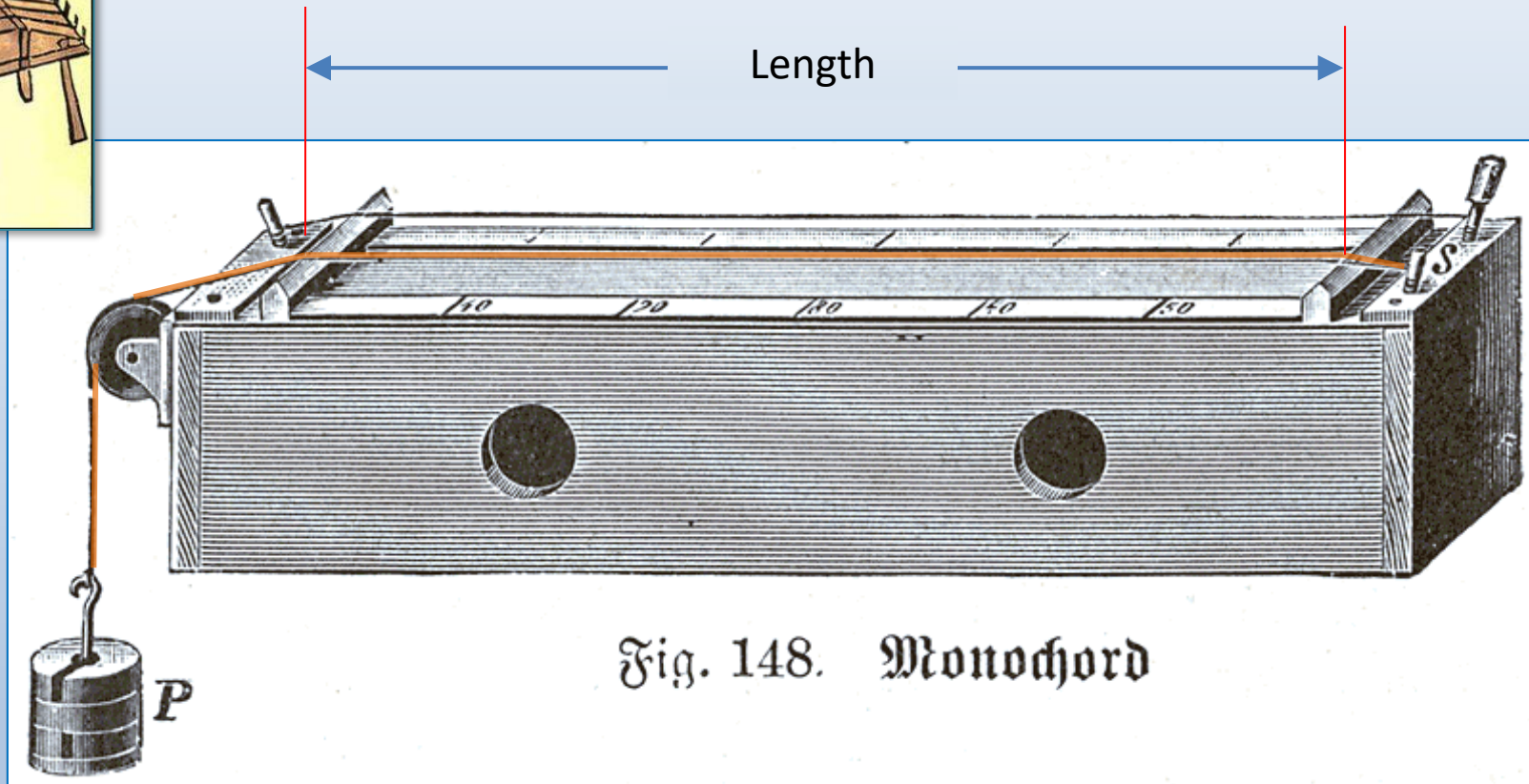


# The Monochord





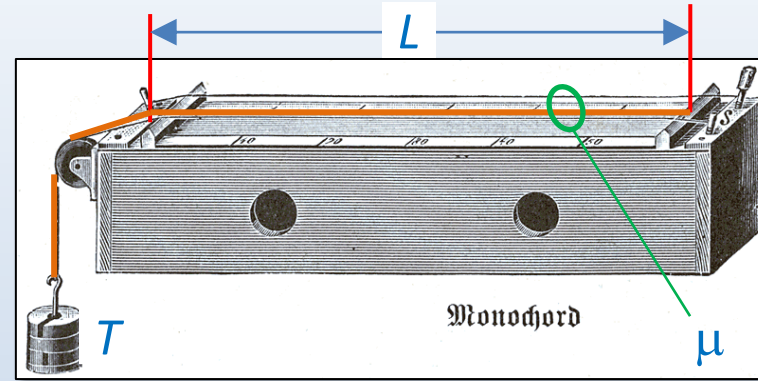
# The Monochord





# Mersenne's Laws of Strings

$$f_0 = \frac{1}{2L} \sqrt{T/\mu}$$

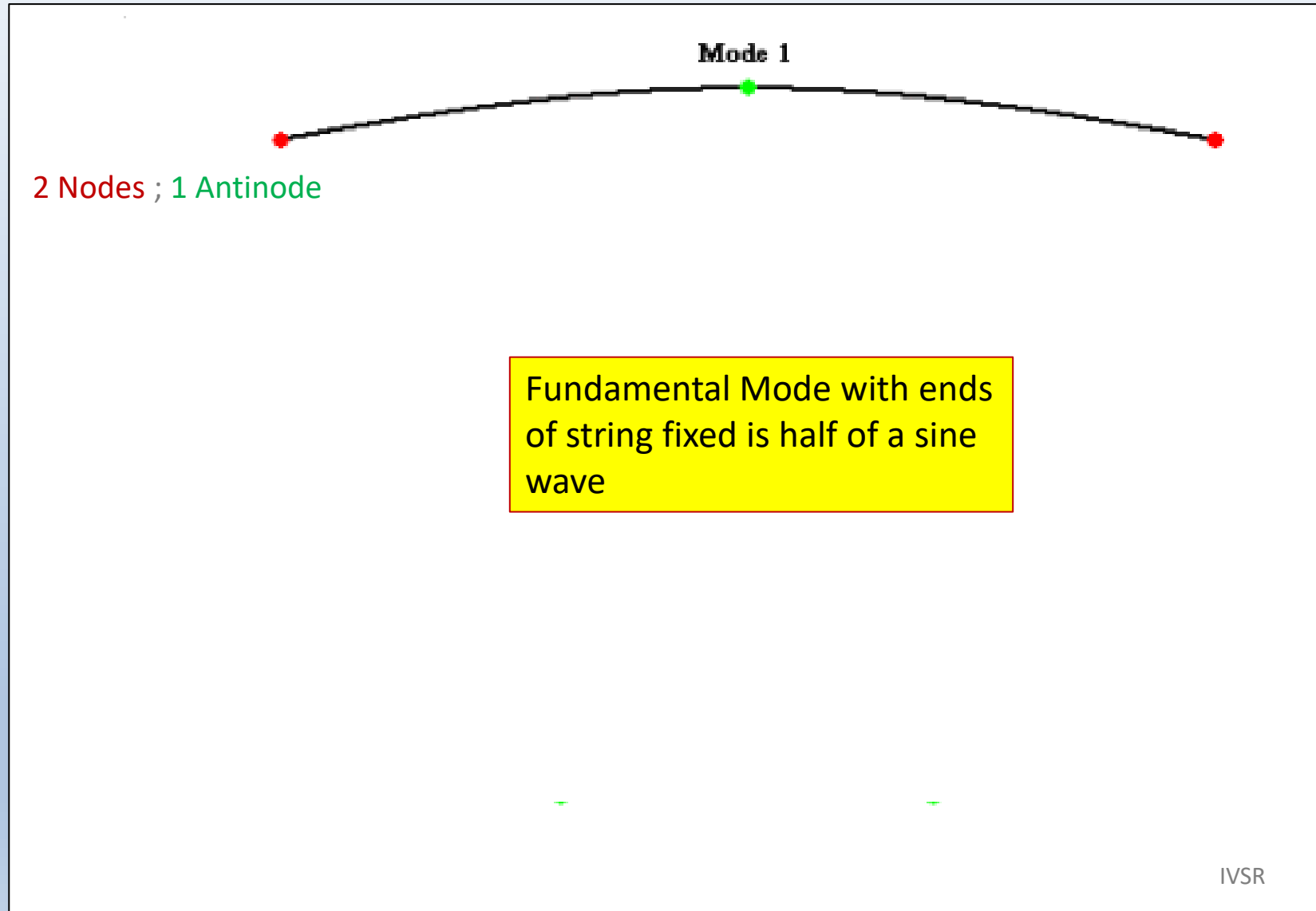


Frequency  $f$  depends on Length  $L$ , Tension Force  $T$ , and String Mass/length  $\mu$ :

- $f_0 \propto \mathbf{1 / L}$  inversely proportional to length
- $f_0 \propto \sqrt{\mathbf{T}}$  proportional to *square root* of tension
- $f_0 \propto \mathbf{1 / \sqrt{\mu}}$  inversely proportional to *square root* of mass per unit length ('fatness')



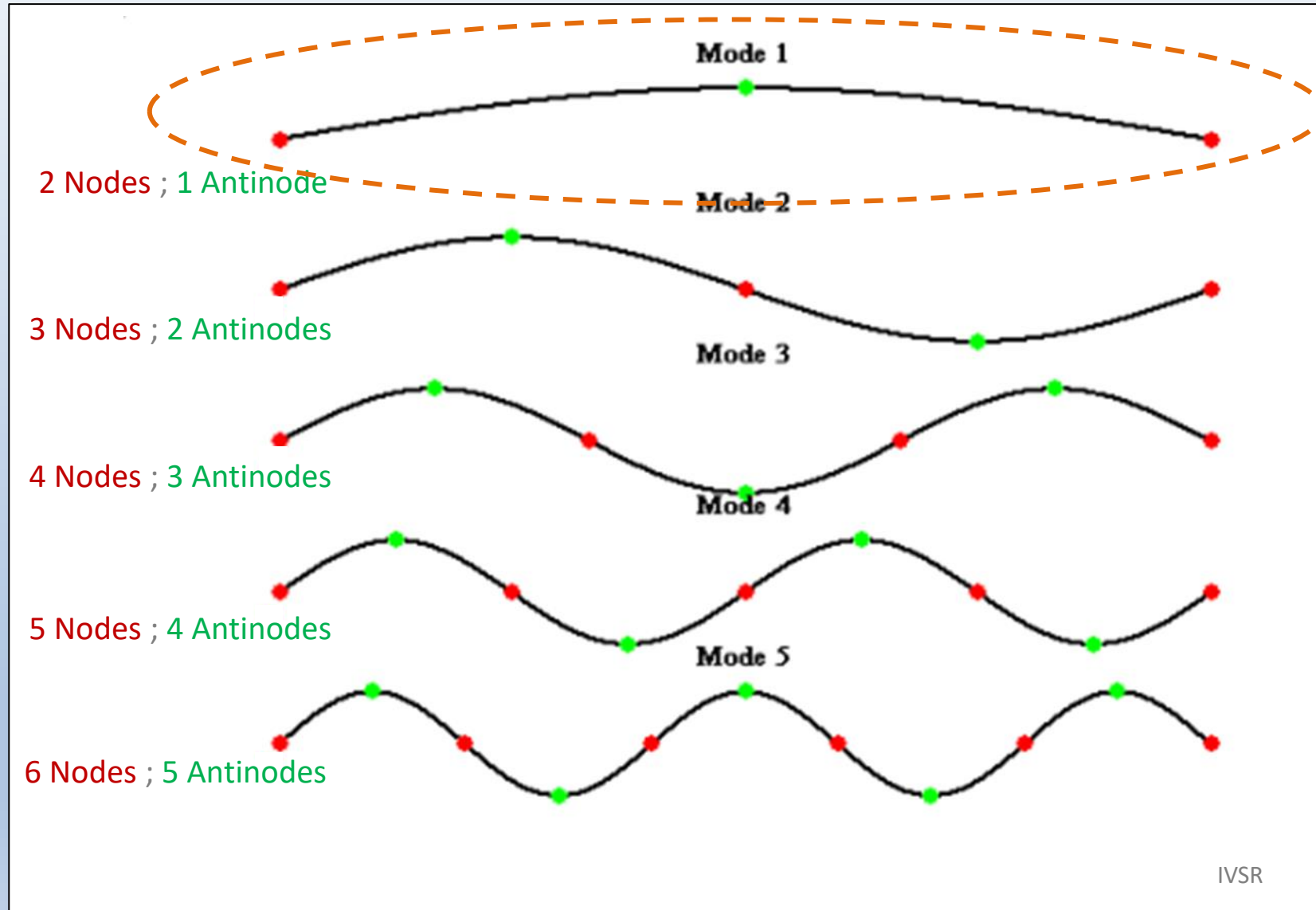
# Possible Pure String Modes



*f* Fundamental



# Possible Pure String Modes



$f$  Fundamental

$2f$

$3f$

$4f$

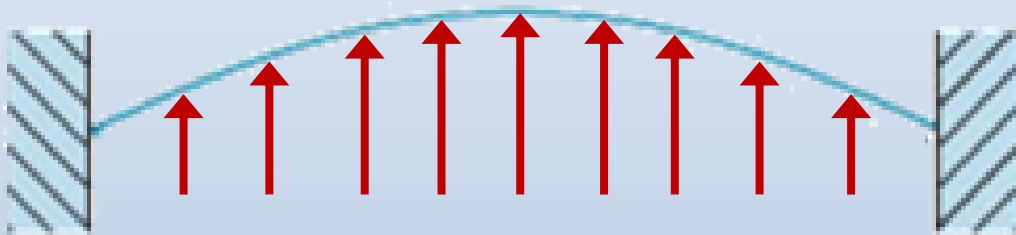
$5f$

Harmonics



# Try to Launch the Fundamental Mode:

Sine shape



Carefully pull string up into a half-sine shape at many points.....

then let go to launch the fundamental mode

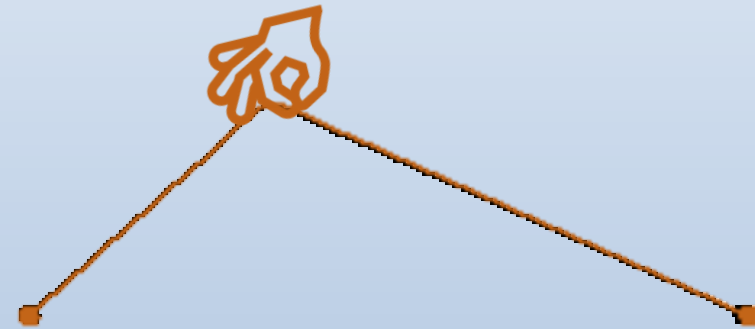


# Try to Launch the Fundamental Mode:

Sine shape



But we actually pluck a triangle ...



Many modes  
superimposed!



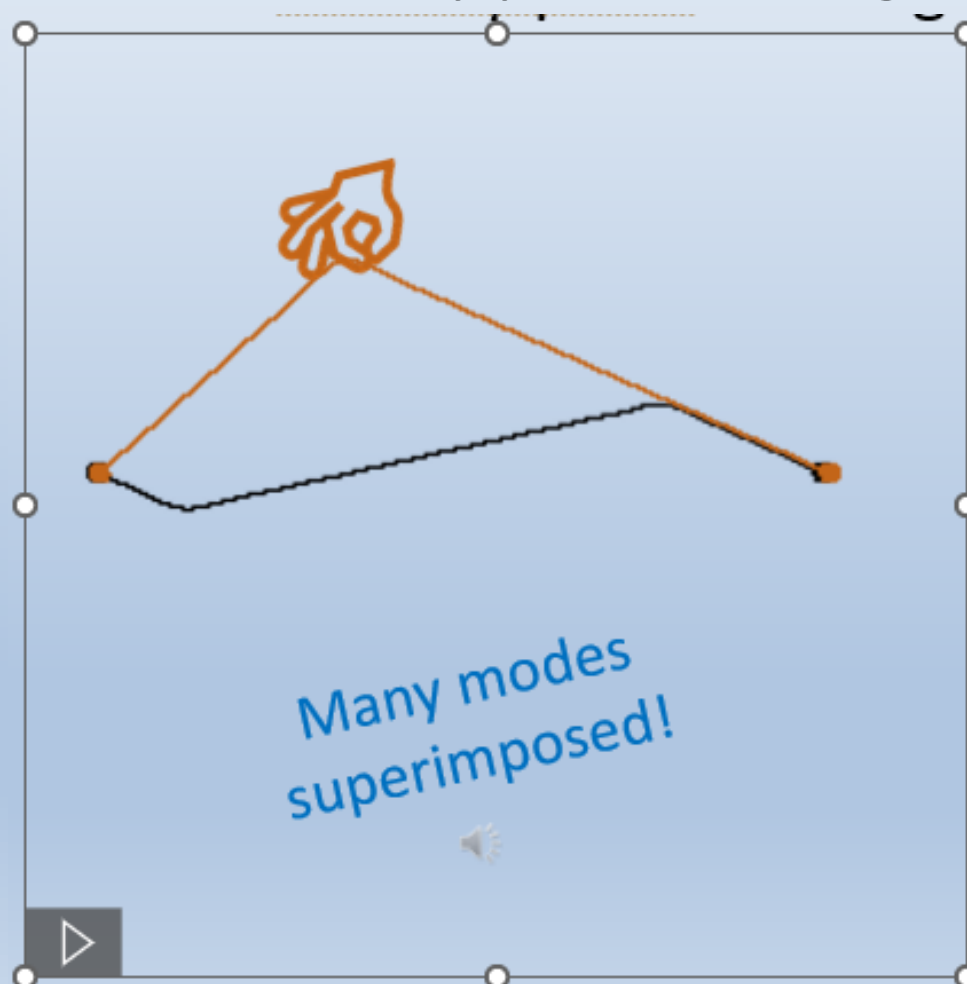


# Try to Launch the Fundamental Mode:

Sine shape



But we actually pluck a triangle ...



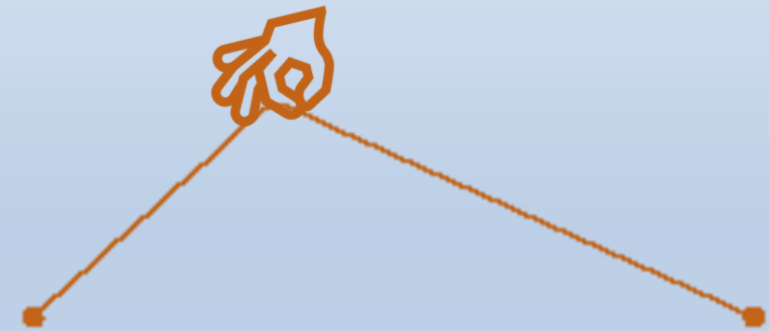


# Try to Launch the Fundamental Mode:

## Plucked String in Slo-Mo



Dan Russell, Kettering/Penn State  
(2011)



Many modes  
superimposed!

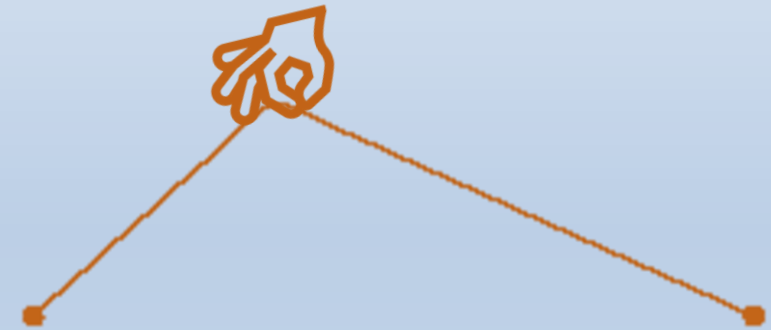


# Try to Launch the Fundamental Mode:

## Plucked String in Slo-Mo



Dan Russell, Kettering/Penn State  
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Many modes  
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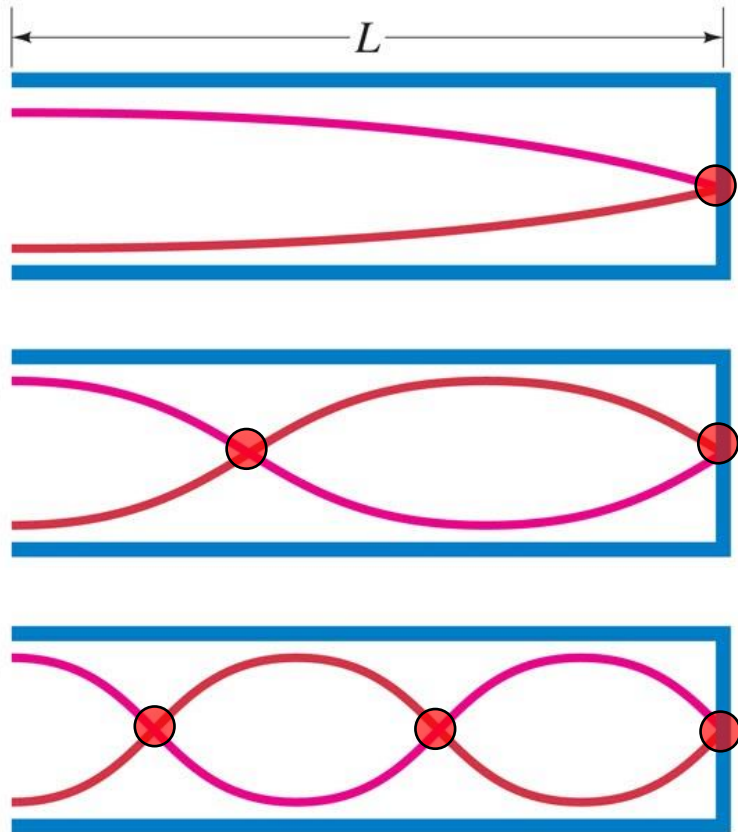


e.g., Clarinet



# Organ Pipe – One Closed End

Air Displacement



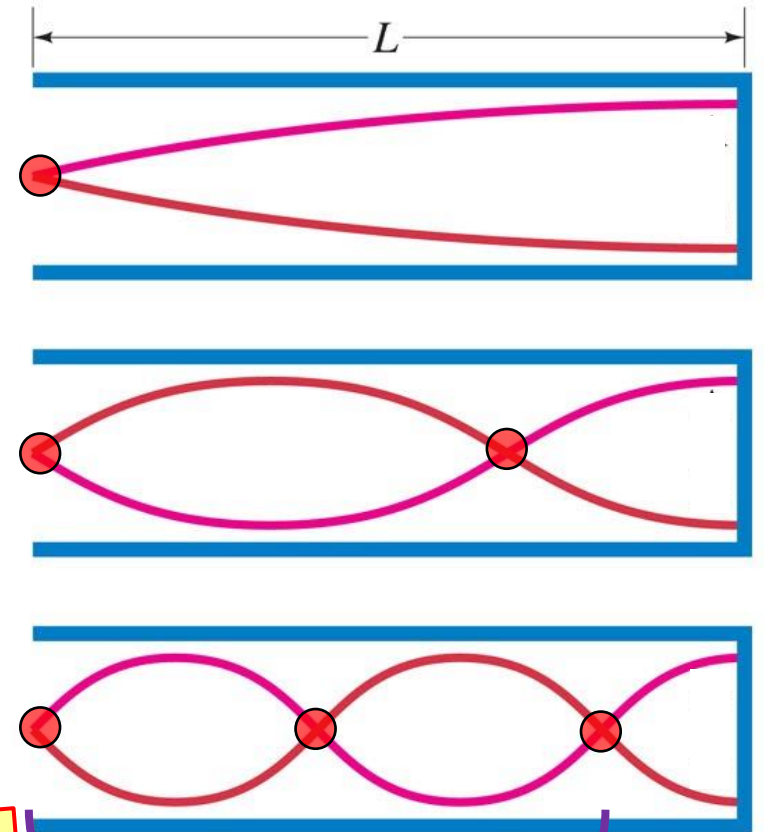
Fundamental Mode  
 $\lambda = 4L$

Third Harmonic  
 $\lambda = (4/3)L$

Fifth Harmonic  
 $\lambda = (4/5)L$

Pressure

in the air



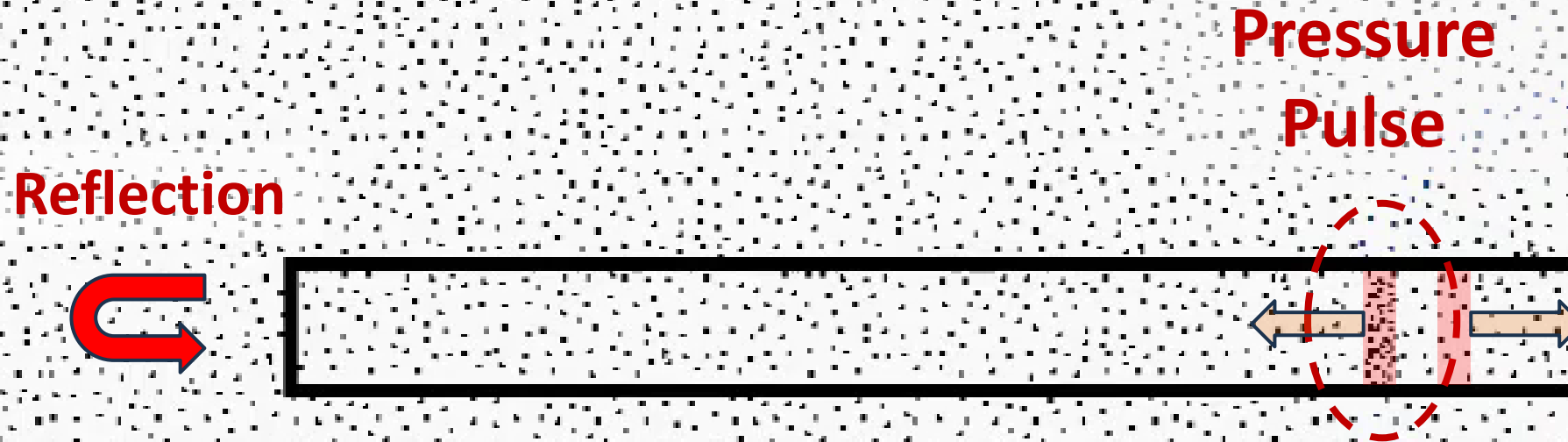
Standing Sound Waves  
in the Pipe

$\lambda_5$

$\lambda_5$



# Illustration of Wave Reflections at Ends of Pipe



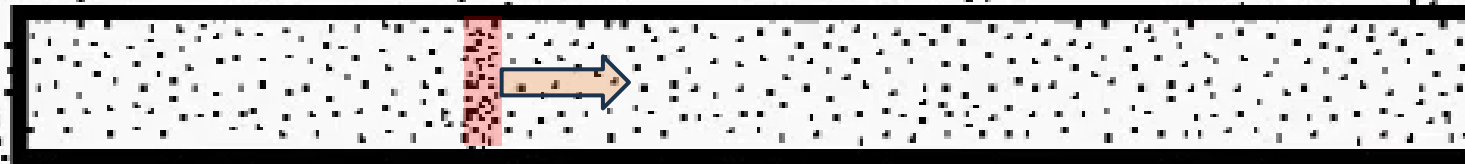
Will reflect from closed end without inversion...

music acoustics at UNSW

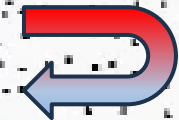


# Illustration of Wave Reflections at Ends of Pipe

Reflection



Reflection



Then will reflect from  
open end with inversion...

music acoustics at UNSW

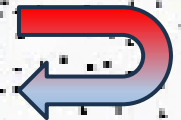


# Illustration of Wave Reflections at Ends of Pipe

Reflection



Reflection



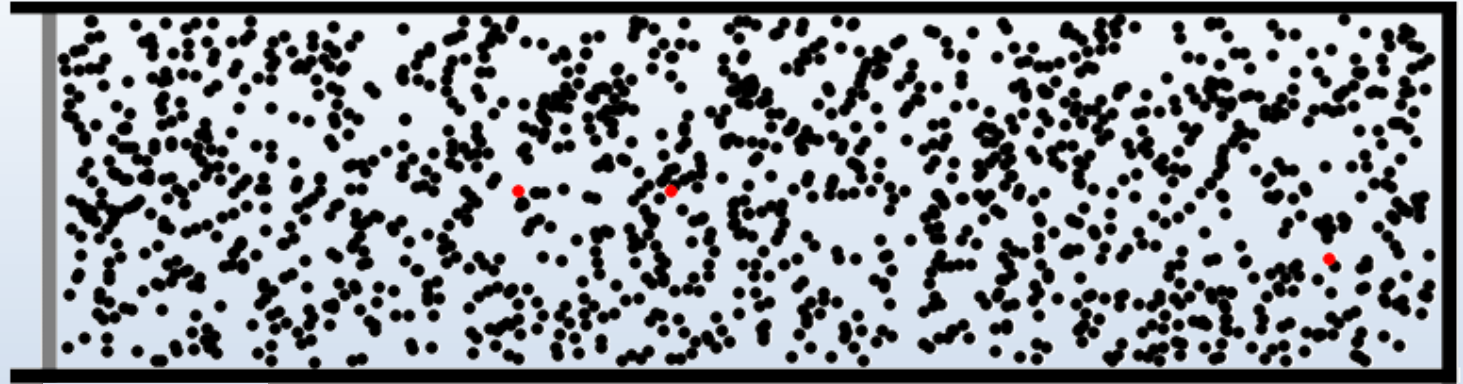
and will then head back as a rarefaction...

music acoustics at UNSW



What's Actually  
Going On?

Open End  
of Pipe →



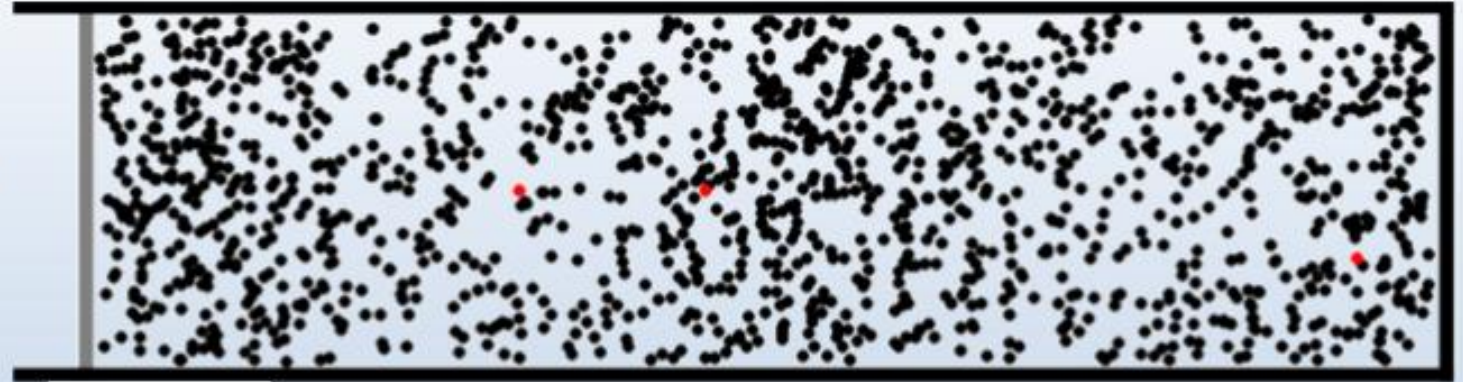
# Open/Closed Organ Pipe: 9<sup>th</sup> Harmonic





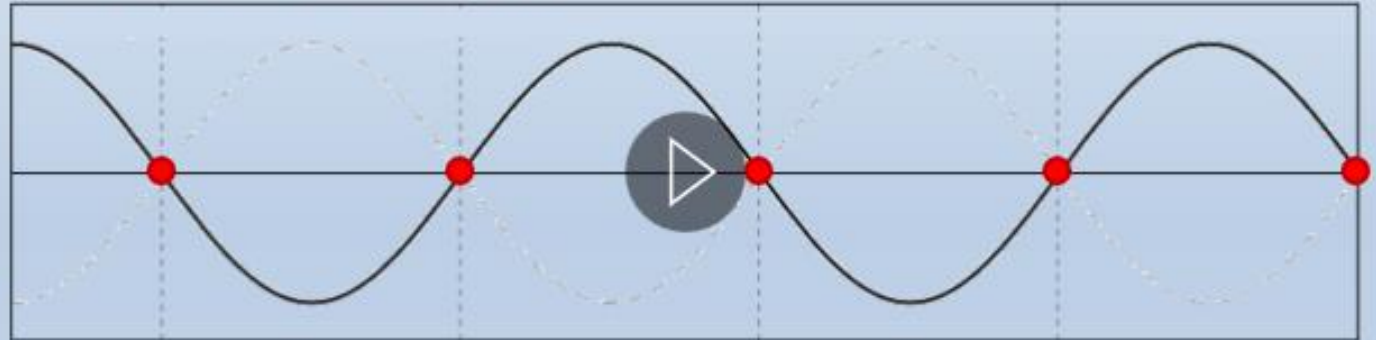
What's Actually Going On?

Open End of Pipe →

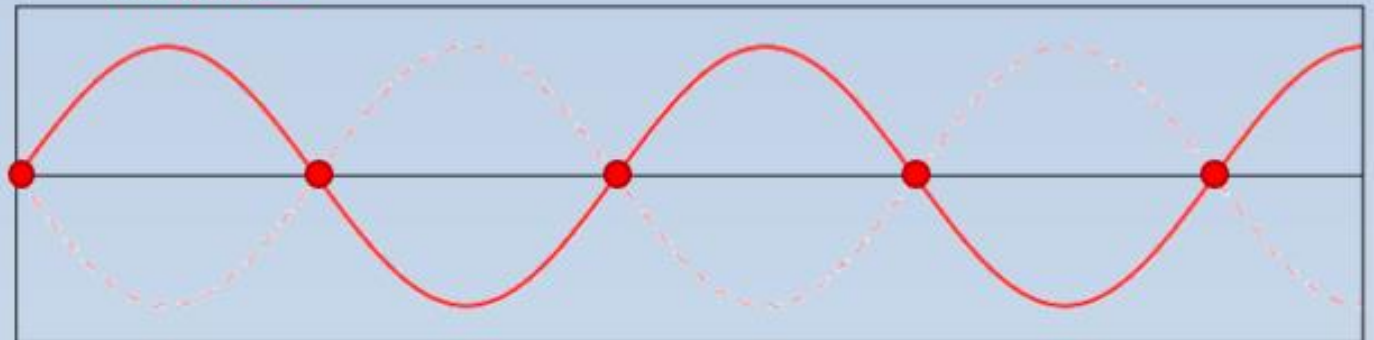


# Open/Closed Organ Pipe: 9<sup>th</sup> Harmonic

Particle Displacement ↔



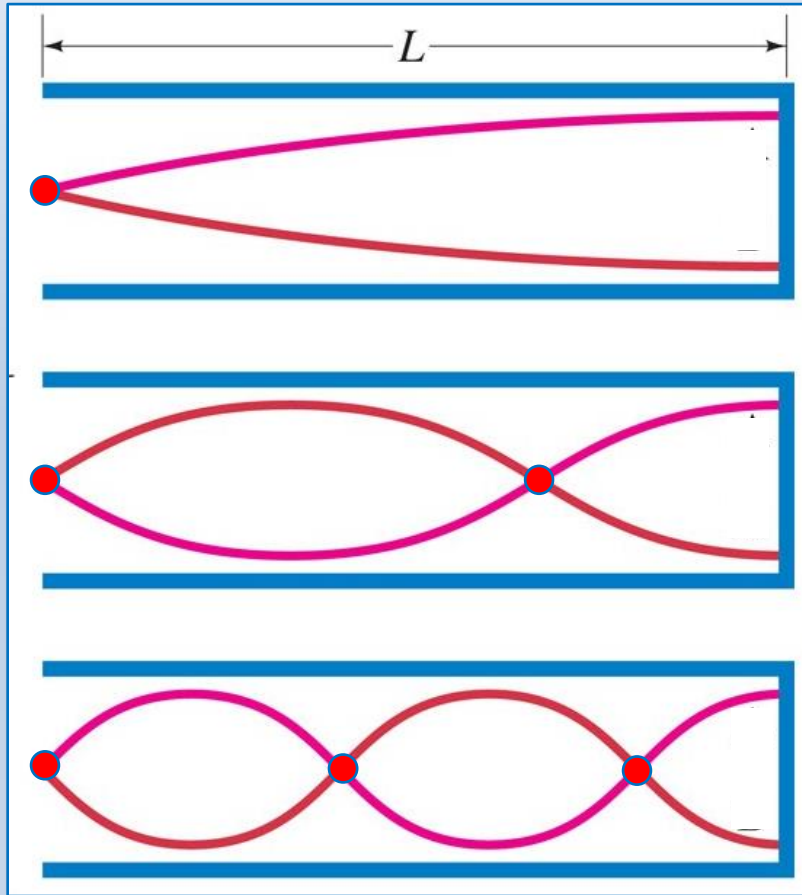
Pressure ↕



# Closed vs. Open Pipe (*Pressure Modes*)

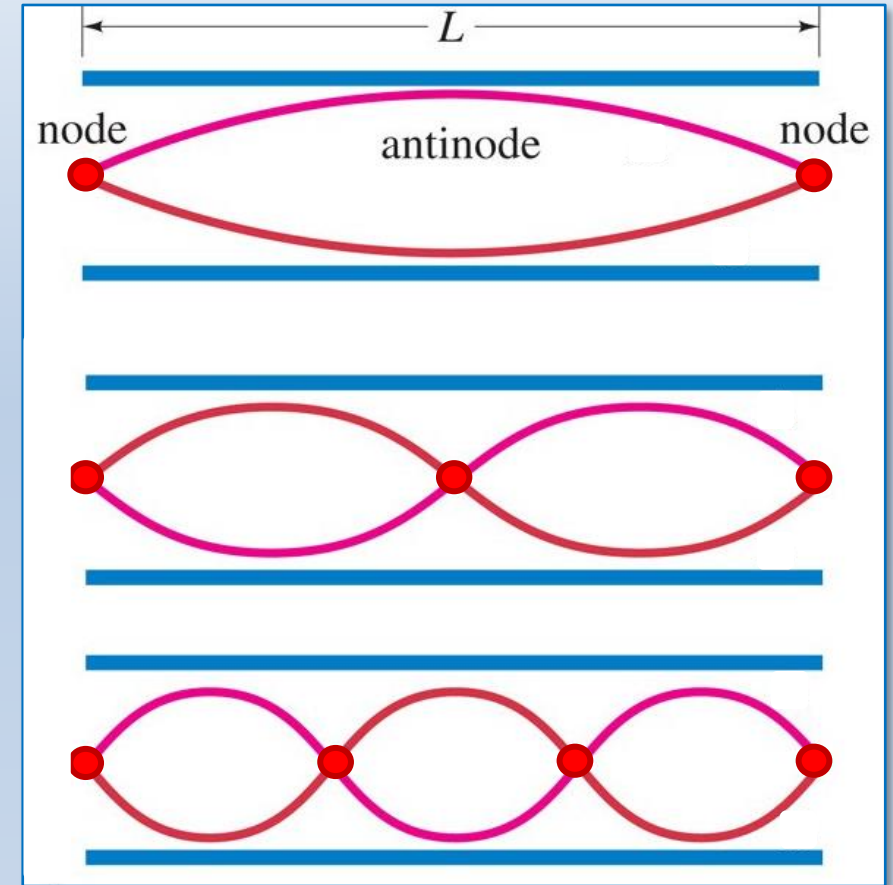
*Closed One End*

Clarinet, e.g.



*Open Both Ends*

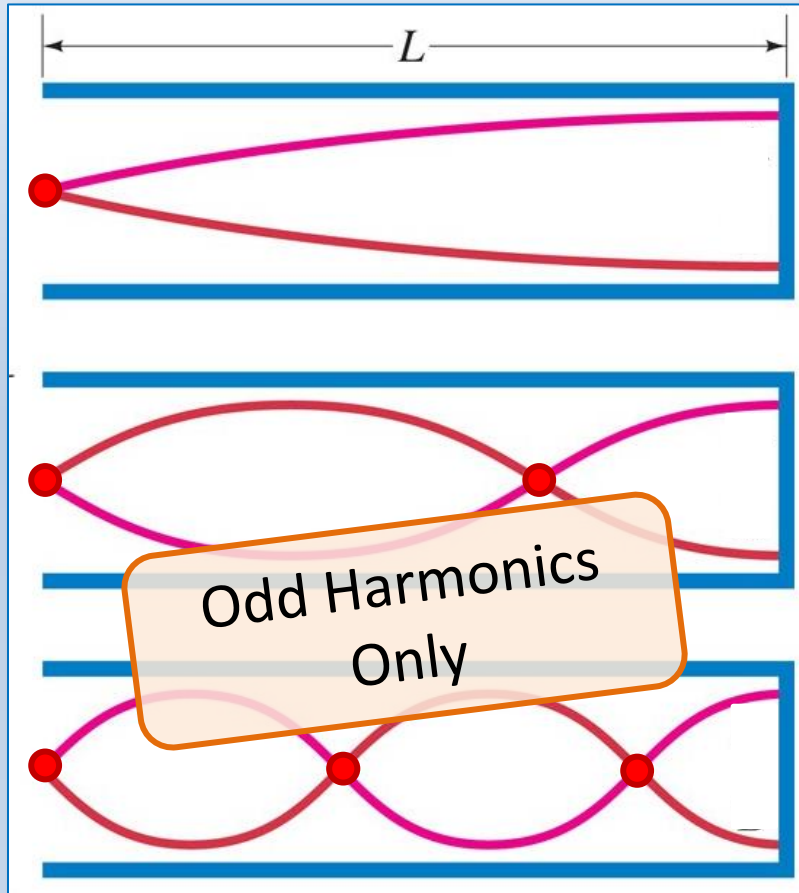
Flute, e.g.



# Closed vs. Open Pipe (*Pressure Modes*)

*Closed One End*

Clarinet, e.g.

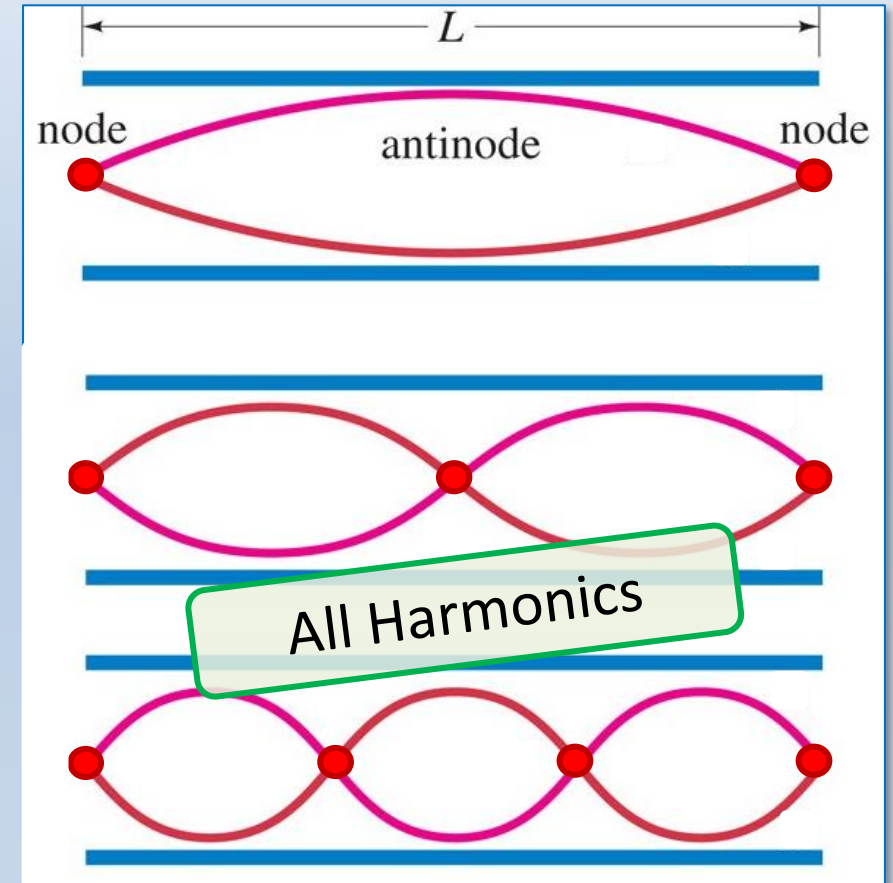


$L = 25''$



*Open Both Ends*

Flute, e.g.



$L = 25''$



$L = 50''$



$$f = v_s / \lambda$$

$$v_s \approx 1100 \text{ ft/s}$$

## Open Pipe

$$L \approx 2.7 \text{ ft}$$

$$\lambda_0 = 2L$$

$$f_0 \approx 200 \text{ Hz}$$

## Demo

(failed)

$$\lambda_1 = L$$

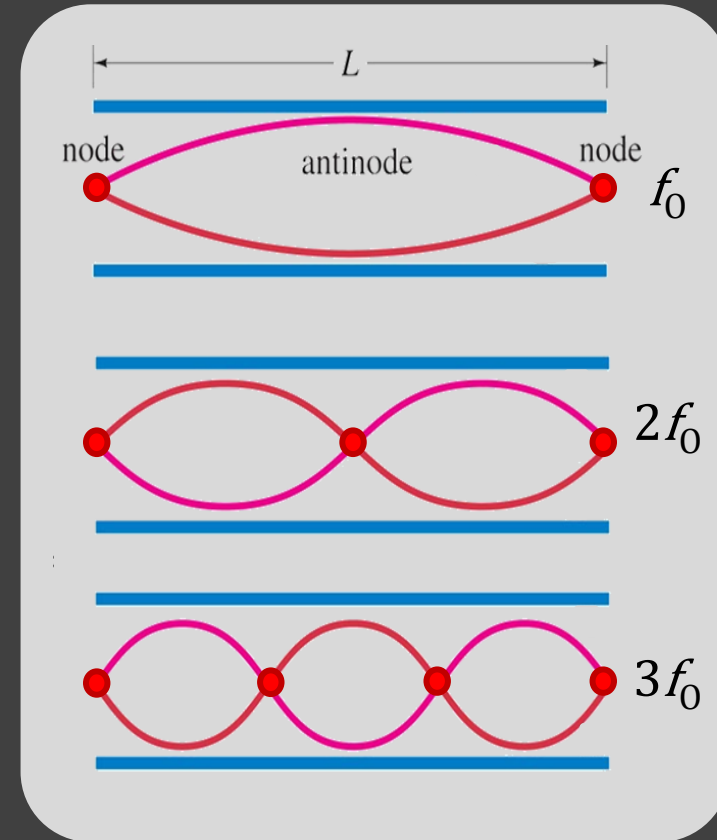
$$f_1 \approx 400 \text{ Hz}$$

$$\lambda_2 = (2/3)L$$

$$f_2 \approx 600 \text{ Hz}$$

$$\lambda_3 = (1/2)L$$

$$f_2 \approx 800 \text{ Hz}$$



$$f = v_s / \lambda$$

$$v_s \approx 1100 \text{ ft/s}$$

Closed Pipe

$\approx 2.7 \text{ ft}$

Demo  
(failed)

$$\lambda_1 = 4L$$

$$f_1 \approx 100 \text{ Hz}$$

$$\lambda_3 = (4/3)L$$

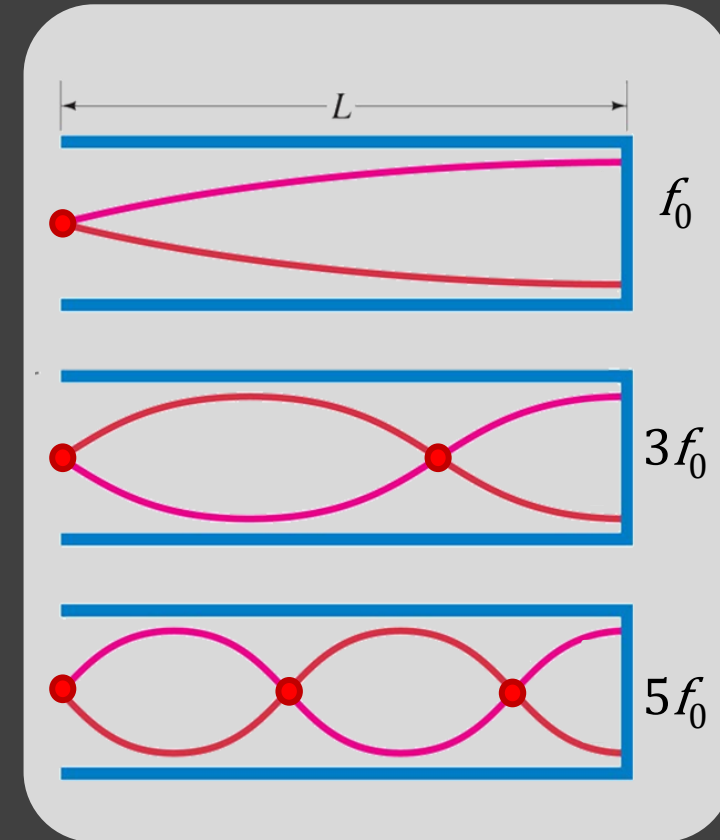
$$f_3 \approx 300 \text{ Hz}$$

$$\lambda_5 = (4/5)L$$

$$f_5 \approx 500 \text{ Hz}$$

$$\lambda_7 = (4/7)L$$

$$f_7 \approx 700 \text{ Hz}$$



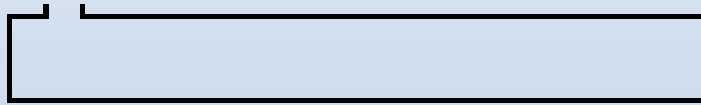
## Question Time

- Helmholtz Resonators
- String Resonators
- Pipes



# Air Column Instrument Examples

Open Cylinder



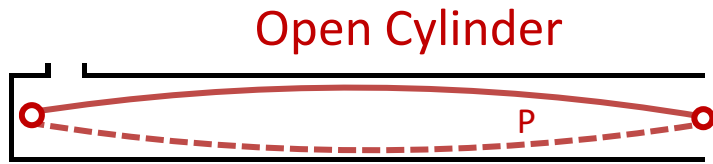
Flute





# Air Column Instrument Examples

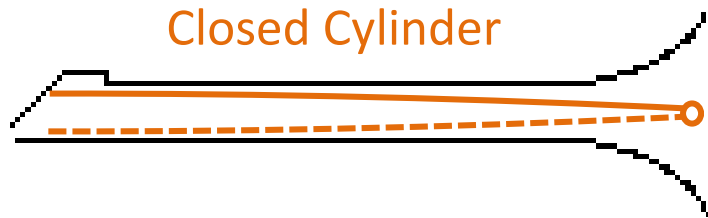
← 2 ft →



1/2 wave

Flute

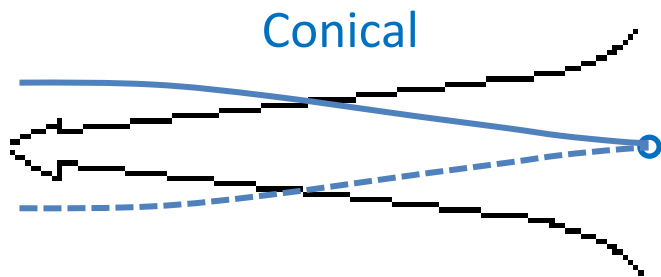
$\lambda_o \approx 4 \text{ ft}$



1/4 wave

Clarinet

$\lambda_o \approx 8 \text{ ft}$



1/2 wave

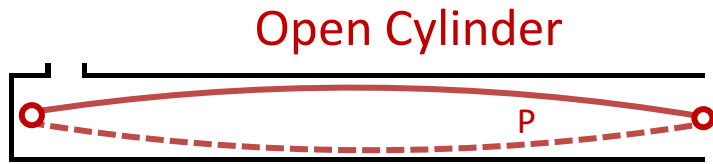
Oboe

$\lambda_o \approx 4 \text{ ft}$



# What About Timbre?

← 2 ft →

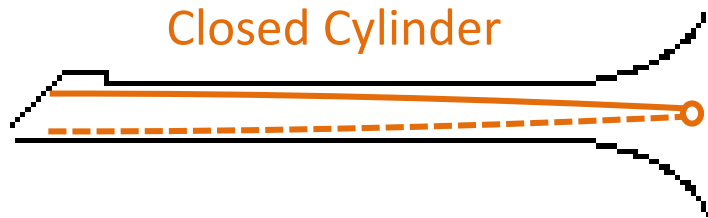


1/2 wave

Flute

All Harmonics

$\lambda_o \approx 4 \text{ ft}$

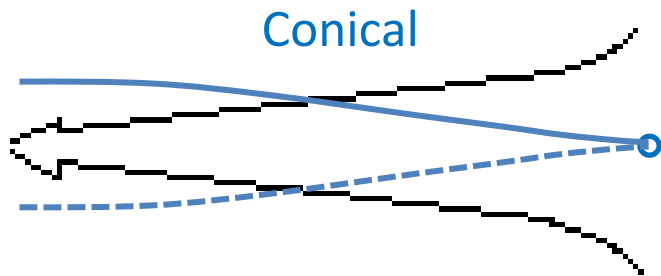


1/4 wave

Clarinet

Odd Harmonics only

$\lambda_o \approx 8 \text{ ft}$



1/2 wave

Oboe

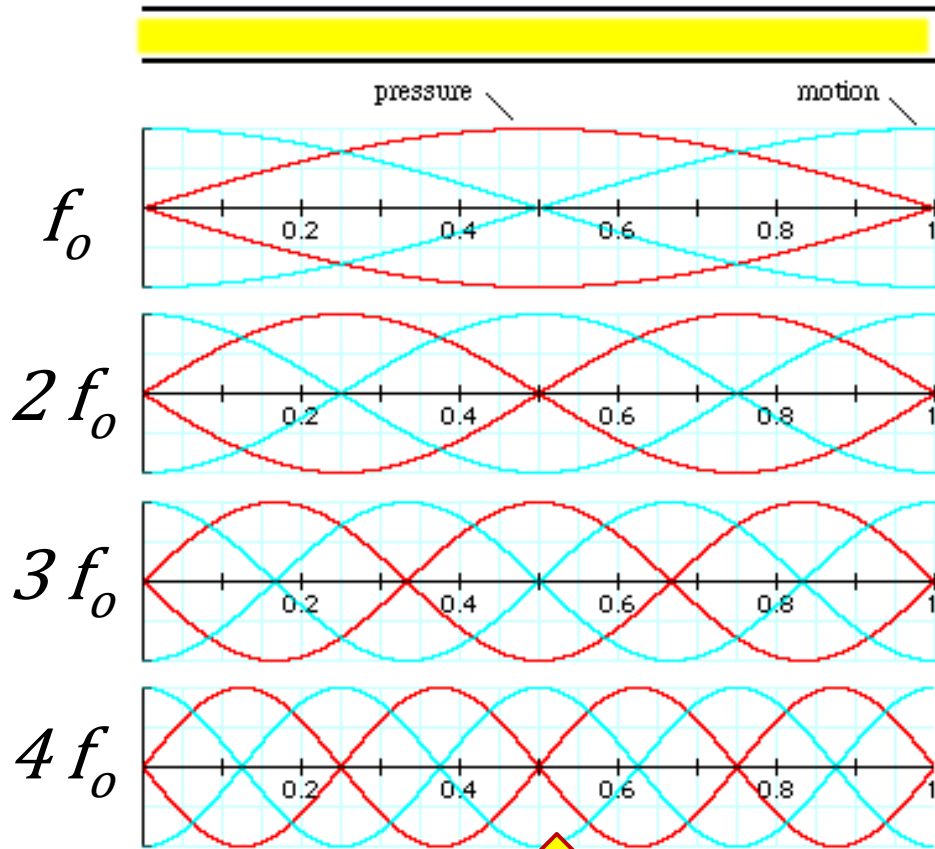
All Harmonics

$\lambda_o \approx 4 \text{ ft}$

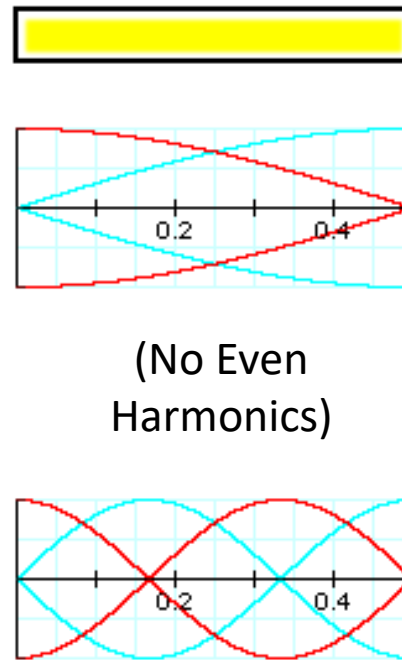


# Comparison of Standing Wave Modes

## Open Cylinder Pipe



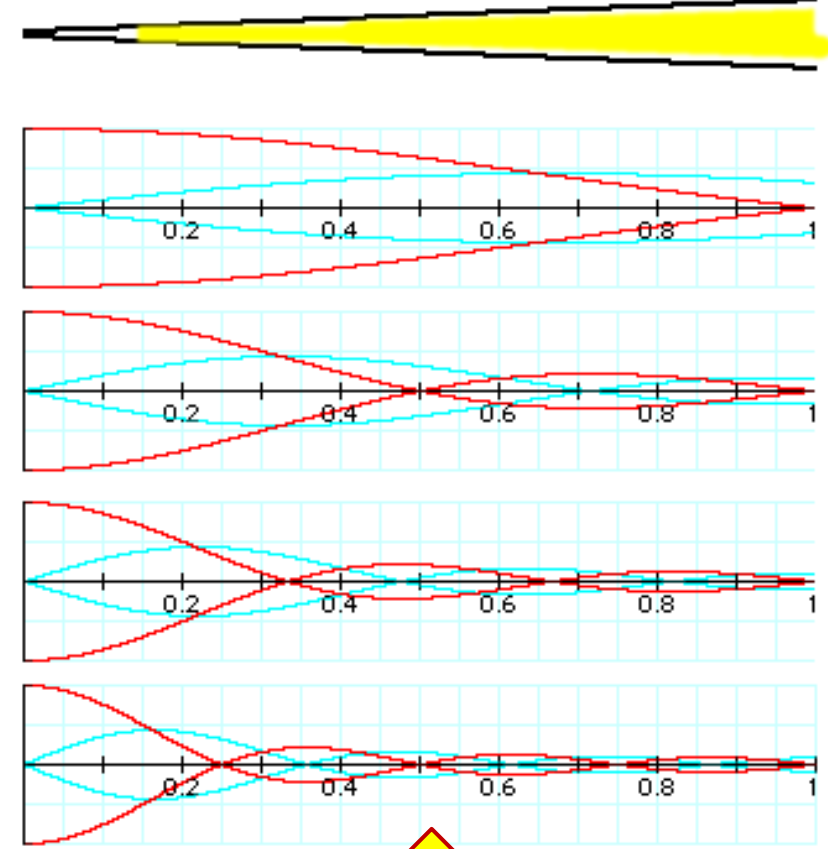
## Closed Pipe



(No Even Harmonics)

(No Even Harmonics)

## Conical Pipe



Same Length,  
Fundamental Frequency,  
and Harmonics

J Wolfe, University of  
New South Wales

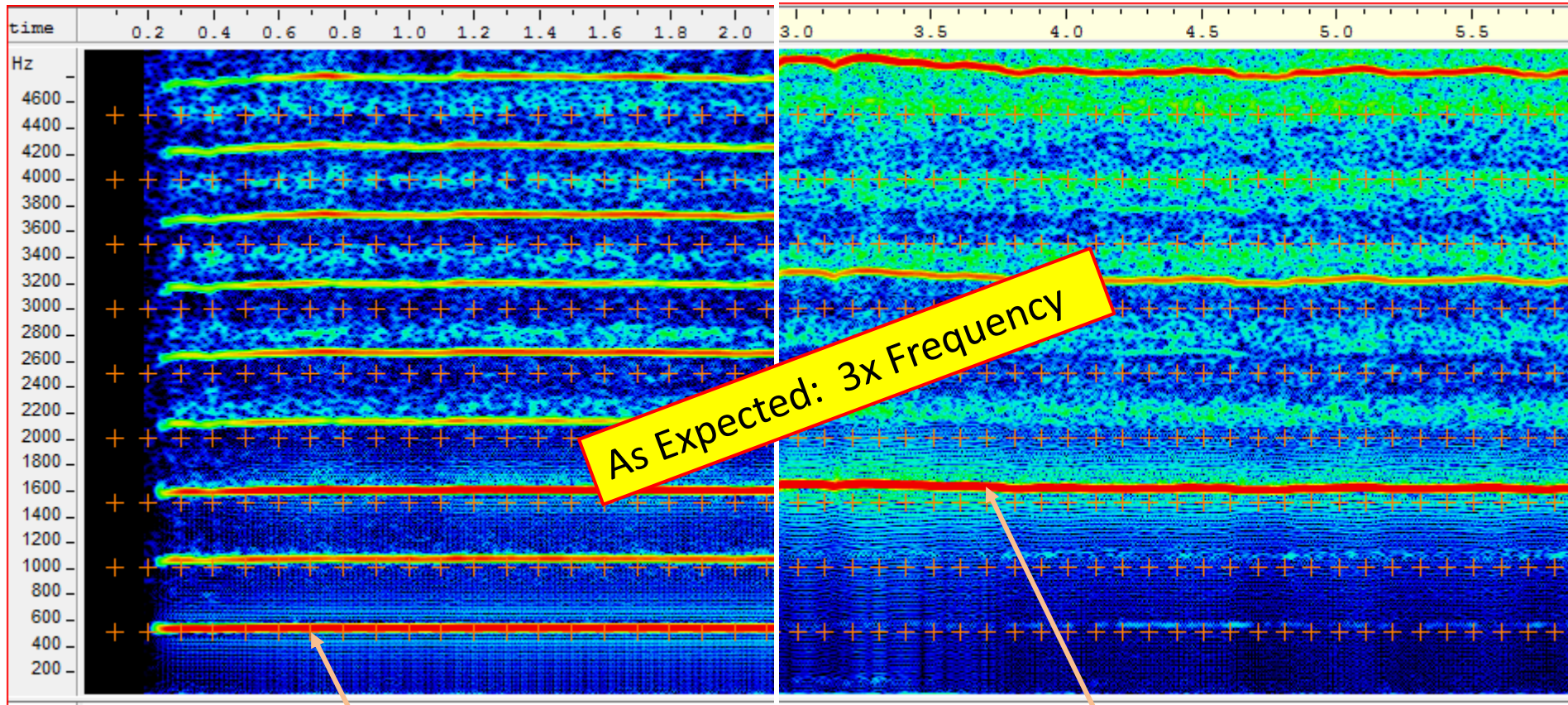
# Recorder Pipe: Air vs. Helium

(All holes closed – base note)

Demo

Air ( $v_s \approx 1100$  ft/s)

Helium ( $v_s \approx 3200$  ft/s)



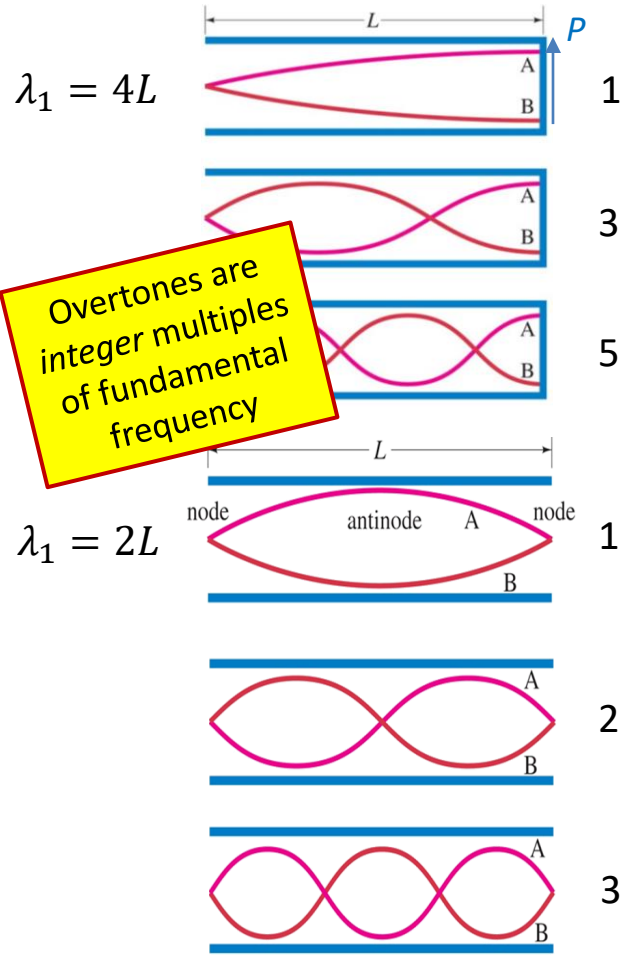
~530 Hz

~1600 Hz



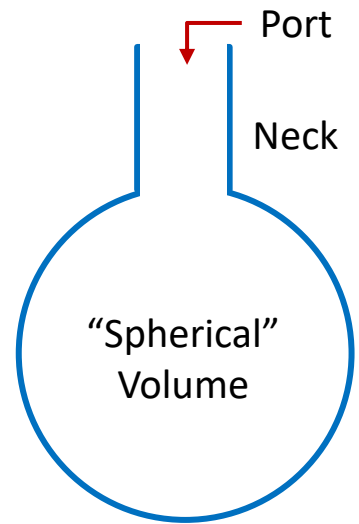
# Resonant Cavities: Augmenting Sounds

## Pipes



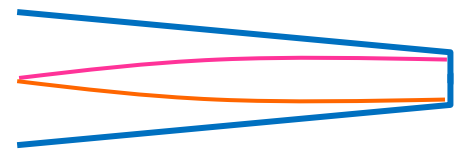
Overtones are integer multiples of fundamental frequency

## Helmholtz Resonators



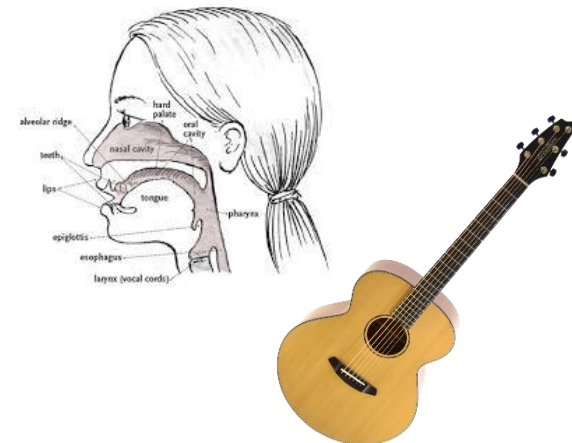
- Mainly has fundamental resonance
- Typically lower frequency than a pipe of similar length

## Irregular Resonators

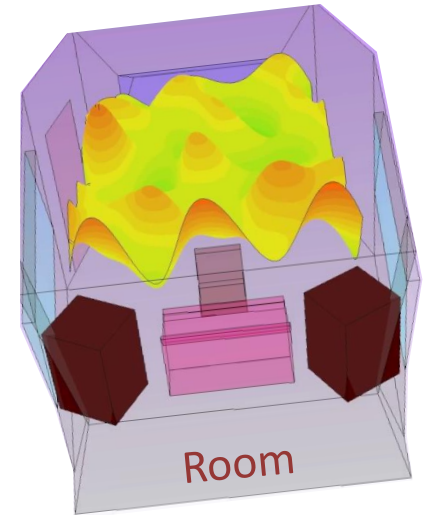


Non-uniform Pipe

- Overtones *may* be integer multiples (e.g. conical)
- Example: Saxophone



# More Complex Resonators



Common Characteristic:  
Modes are generally *not* harmonics of Fundamental



# Singing Prayer Bowl





# Resonant Vibrational Modes of a Wine Glass



# Resonant Vibrational Modes of a Wine Glass



High Speed Camera



# Benjamin Franklin's Glass Harmonica (1761)



Stick/Slip on rotating glass bowls



Thomas Bloch, Paris Music Museum 2007





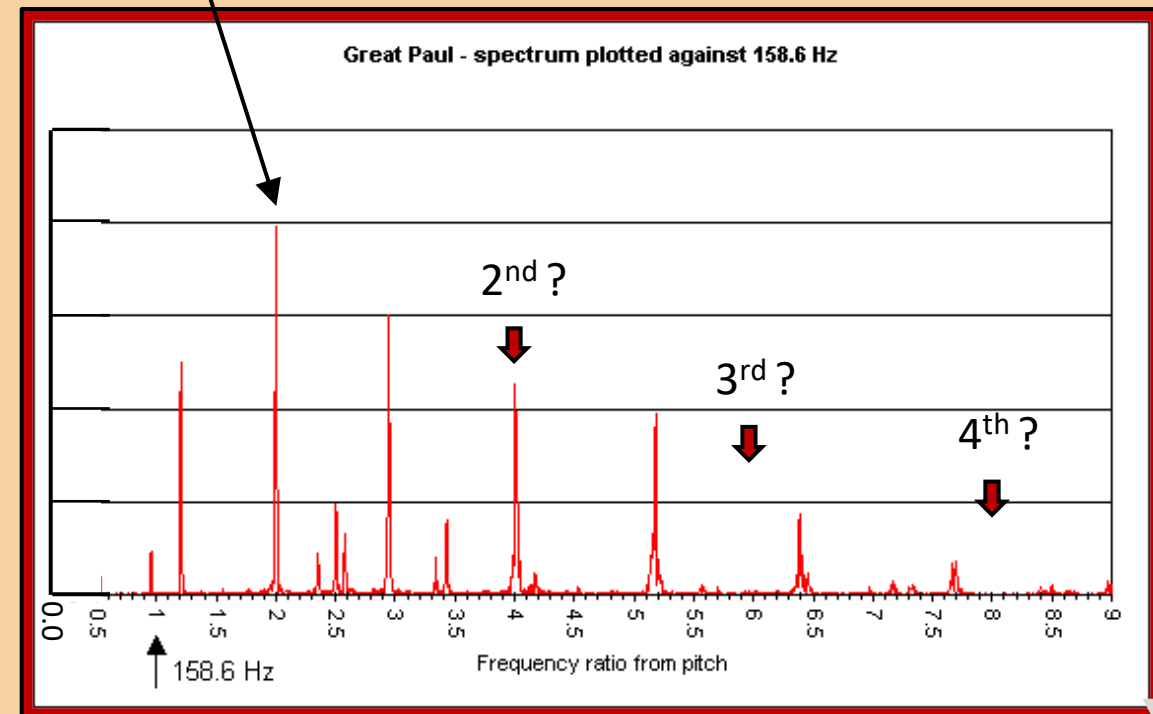
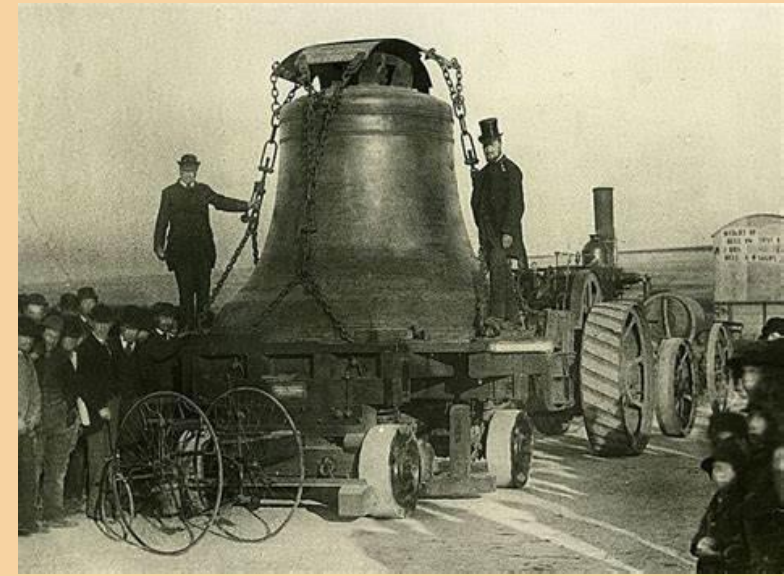


# Great Paul Bell

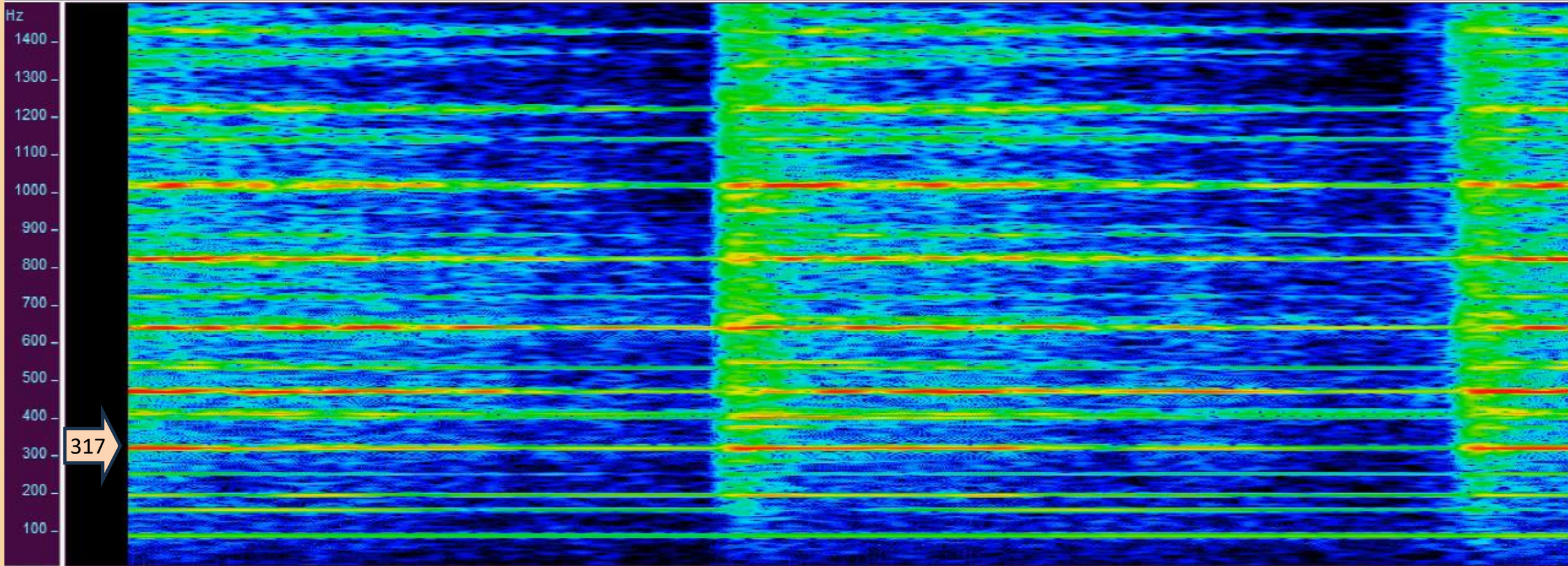
## St. Paul's Cathedral

1882, 17 tons

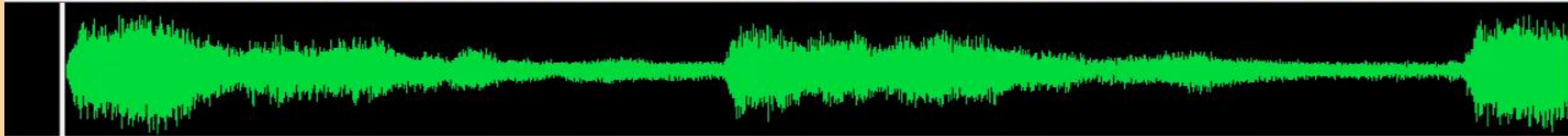
Apparent Pitch:  
317 Hz



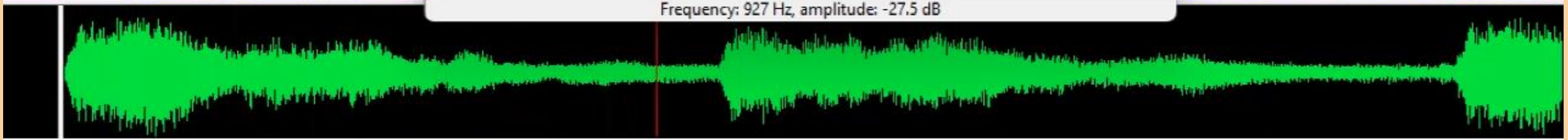
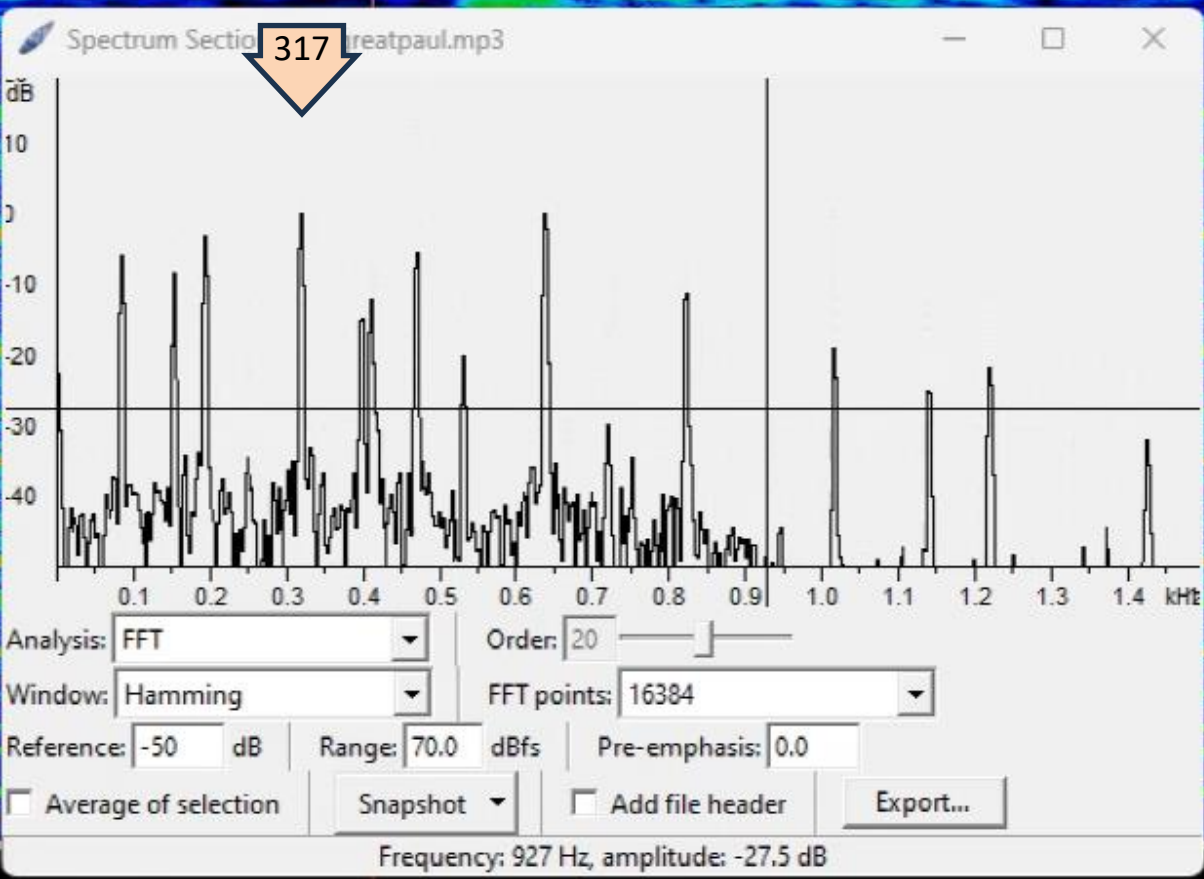
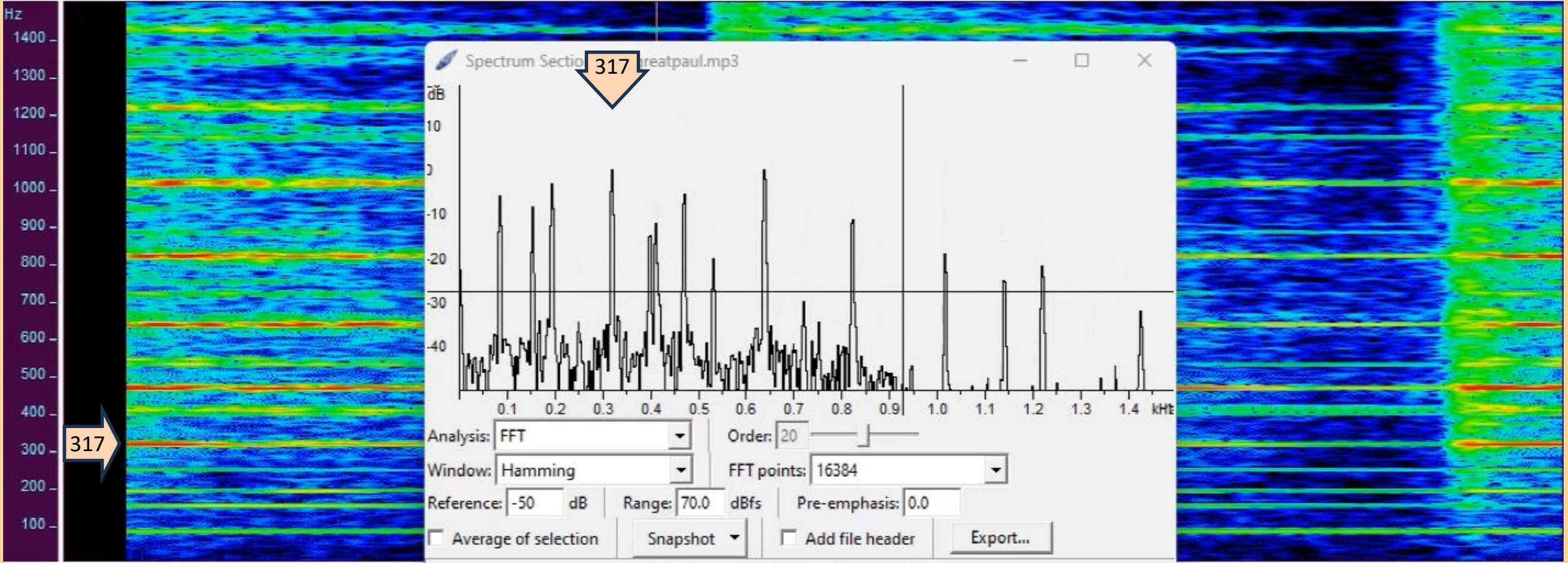




317







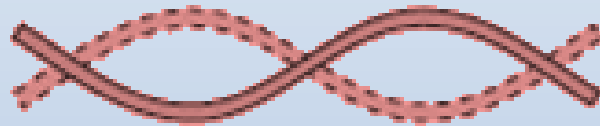
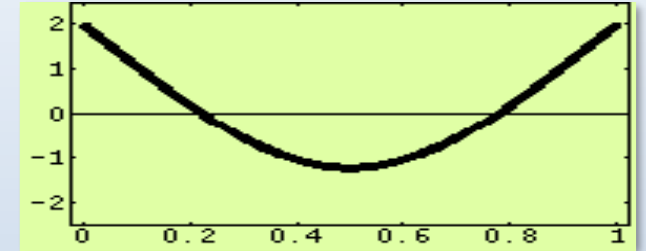
# Vibrating Bars



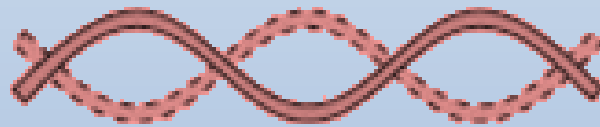
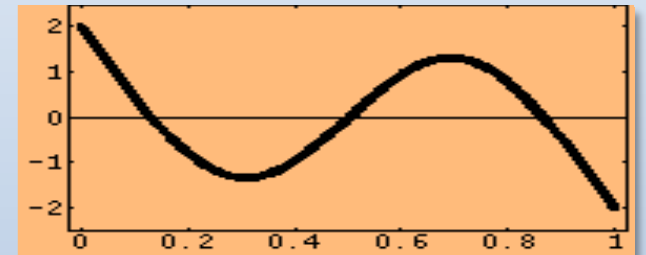
Xylophone  
Rochdale Borough Council, UK  
YouTube (~2020)



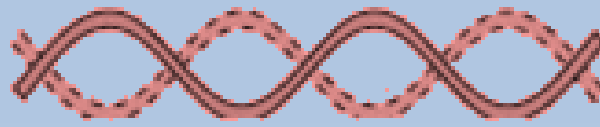
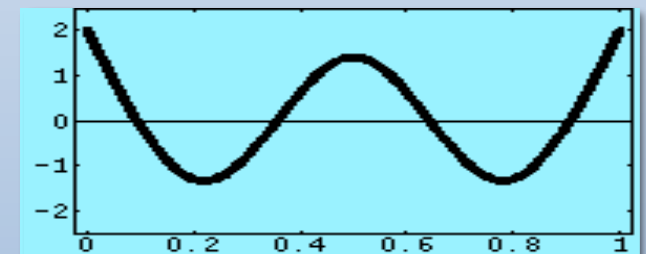
$$f_0$$



$$2.76 f_0$$



$$5.40 f_0$$



$$8.93 f_0$$

Dan Russell  
(Penn State)

Open University [GB]

**Not anywhere near harmonic!**

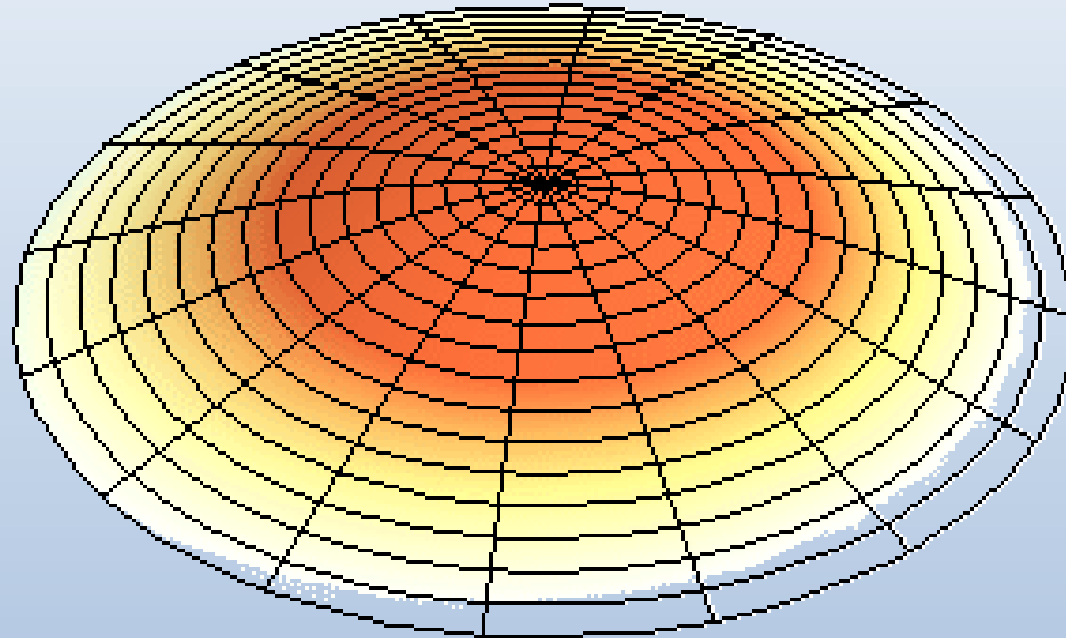




# Drumheads: Two Dimensional Membranes



# Fundamental Mode of a Drumhead (0,1)

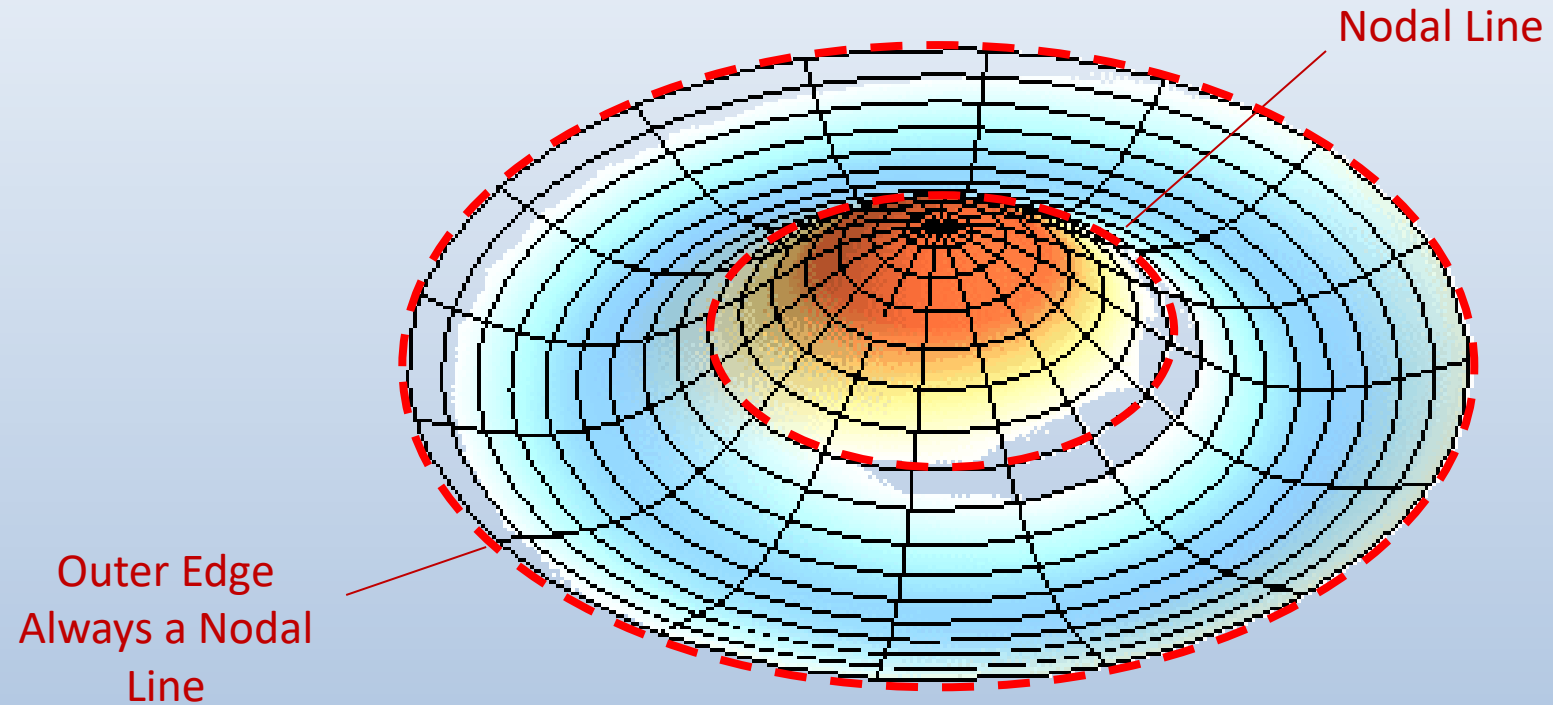


$$f = f_0$$

D Russell Penn State



# The (0,2) Drumhead Mode

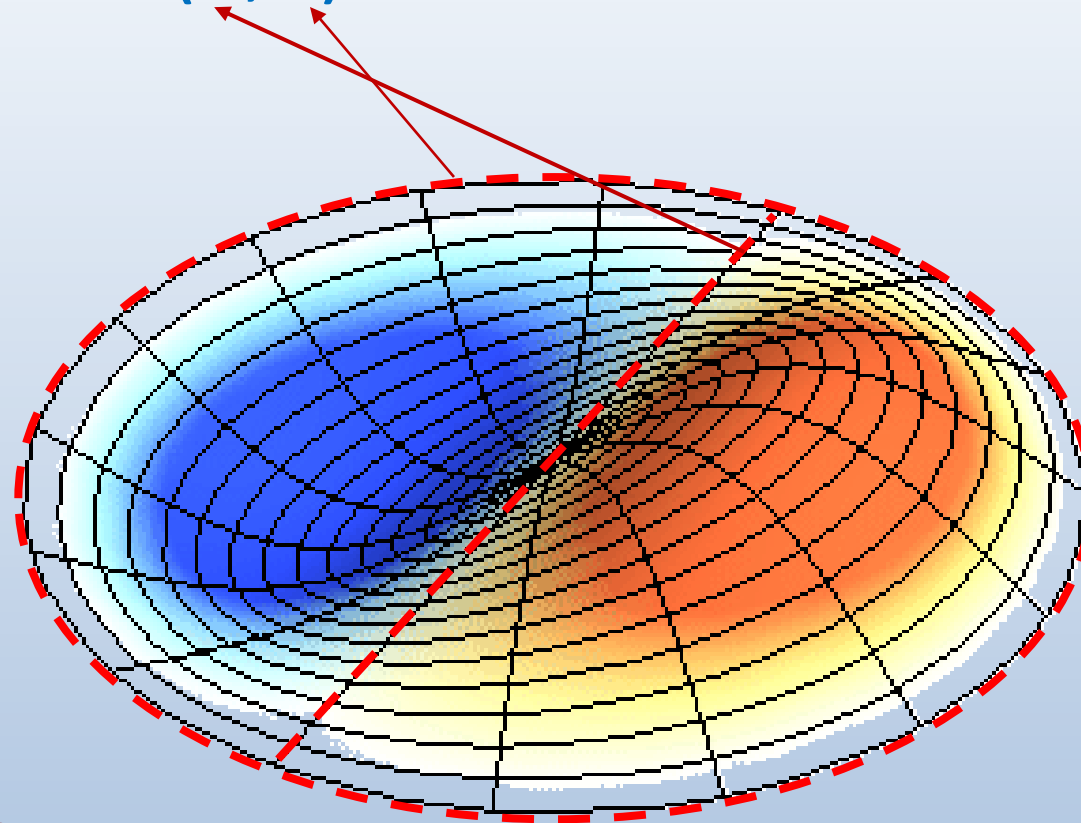


$$f = 2.295 f_0$$

D Russell Penn State



# The (1,1) Drumhead Mode



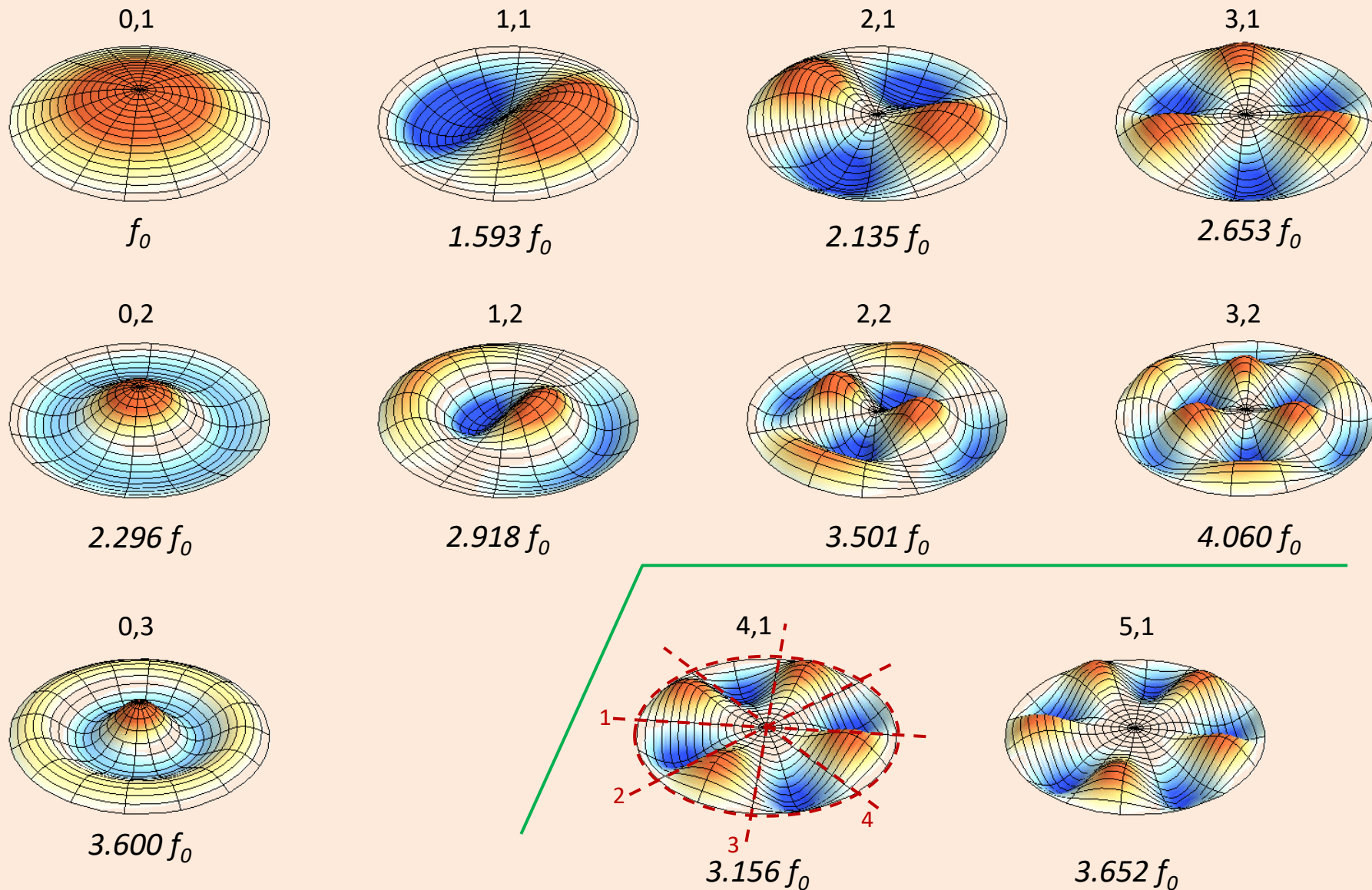
*Symmetric:*  
**No net air volume**  
change under the  
drumhead

$$f = 1.593 f_0$$

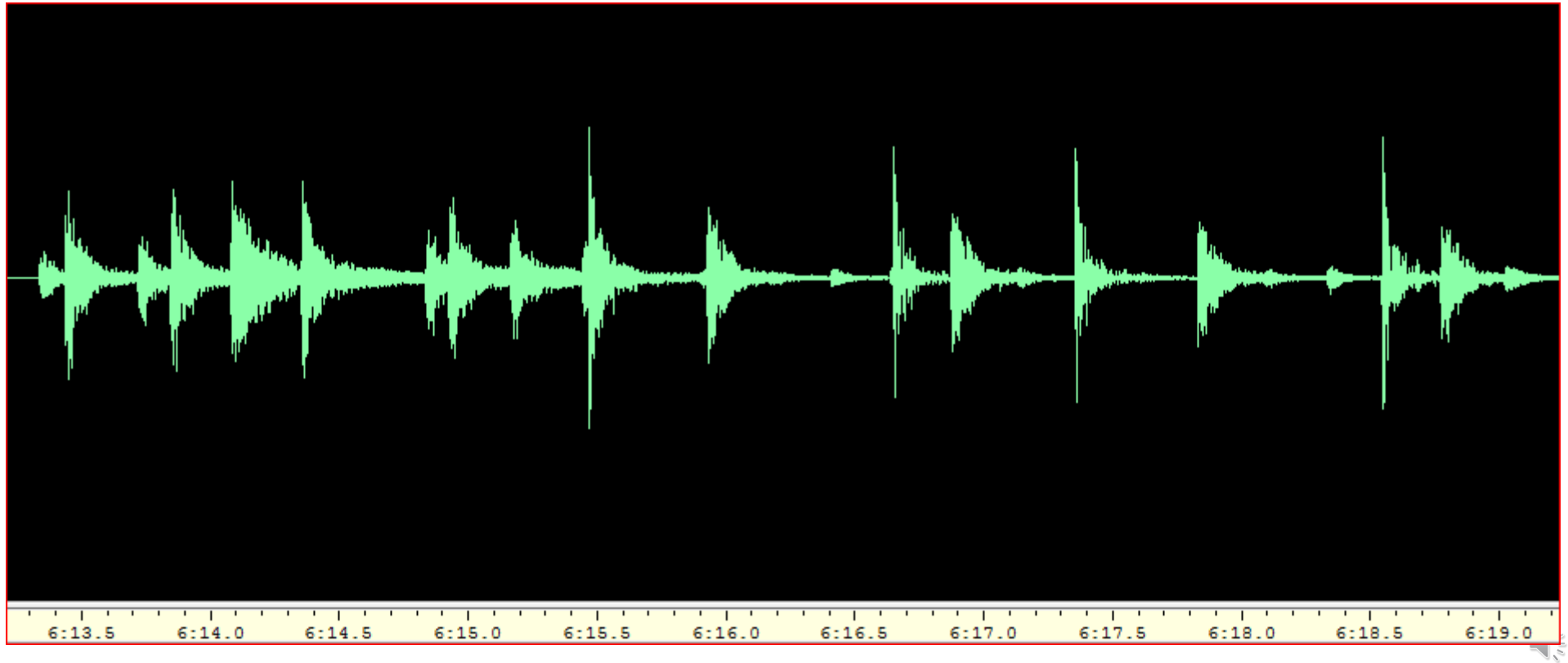
D Russell Penn State



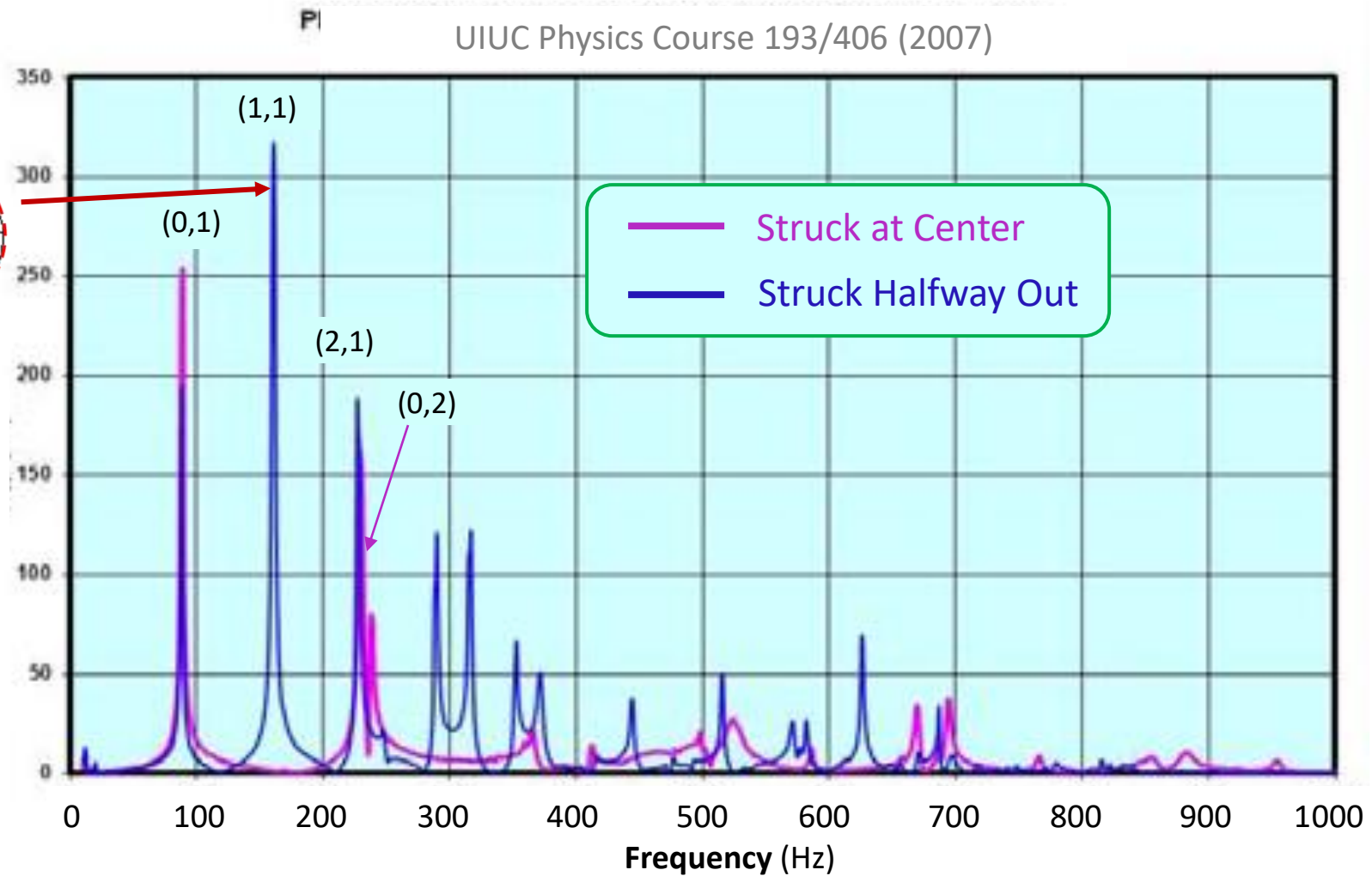
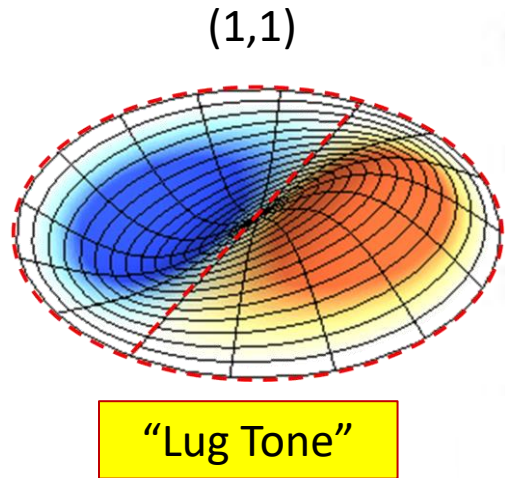
# More Drumhead Modes



# What you're hearing...

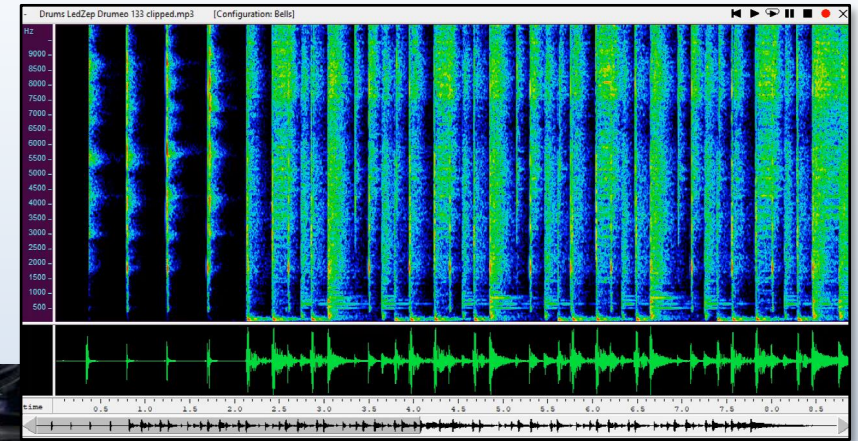


# Measured Sound Spectrum of 12" Tom Drum





Groove from  
Led Zeppelin's  
"Fool In the Rain"  
**Drumeo**  
YouTube ~2021



**1**

#10

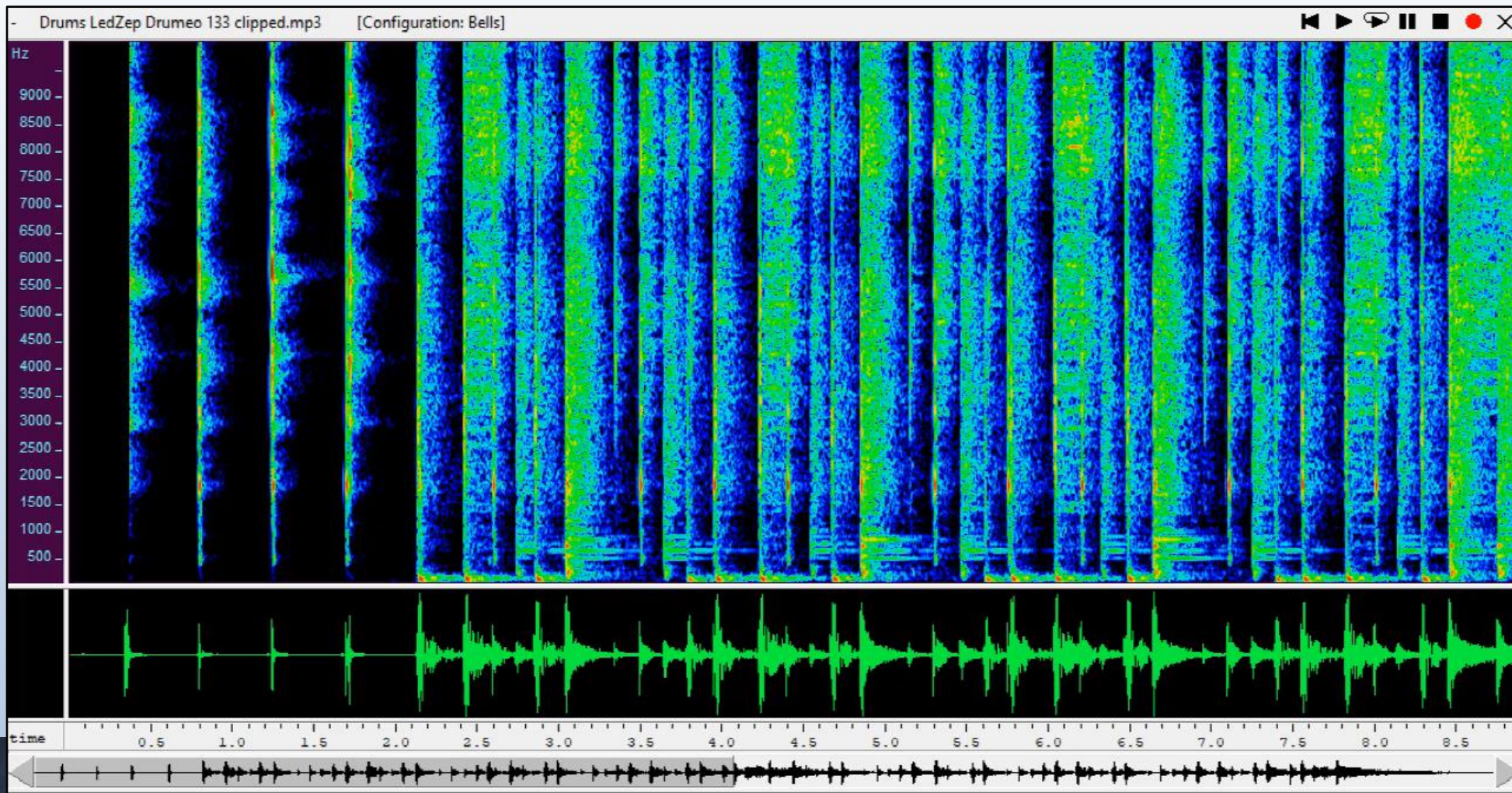




Groove from  
Led Zeppelin's  
"Fool In the Rain"  
Drumeo  
YouTube ~2021

10 kHz

0 Hz



Musical notation for a drum groove, labeled '#10'. The notation is on a single staff and consists of a series of eighth notes with 'x' marks above them, indicating a specific drum pattern. There are four groups of three notes, each with a '3' above it, suggesting triplets. A small blue logo is visible in the bottom right corner of the notation area.

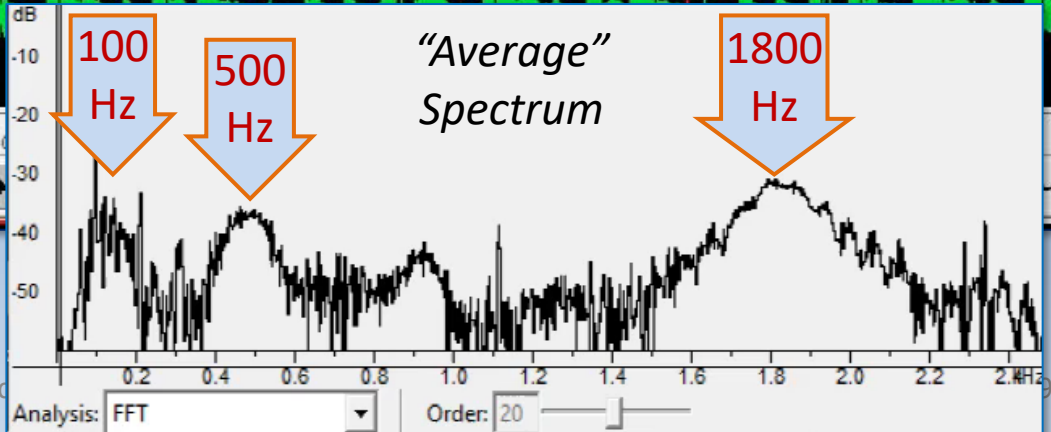
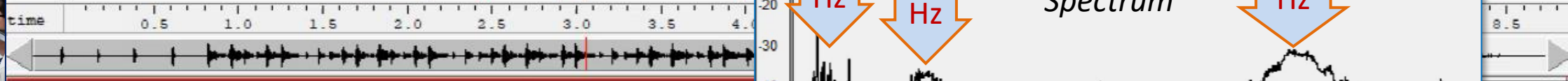
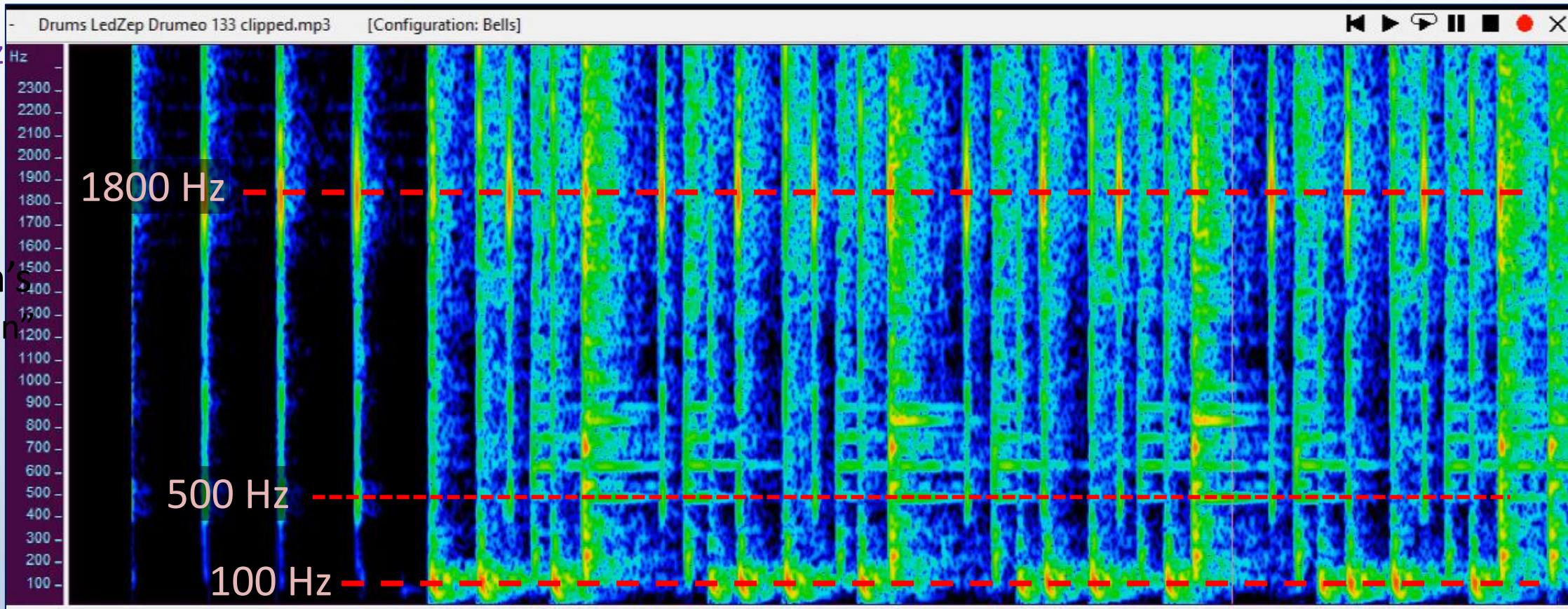




2.5 kHz

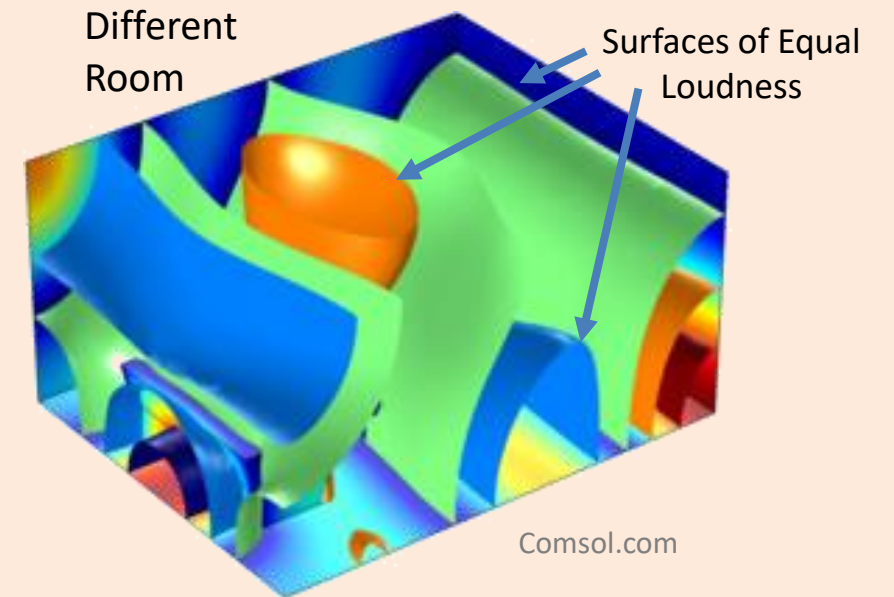
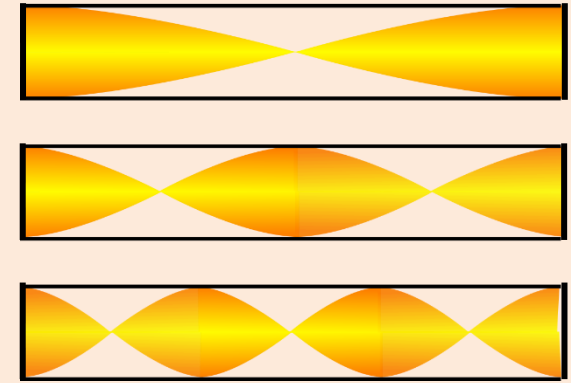
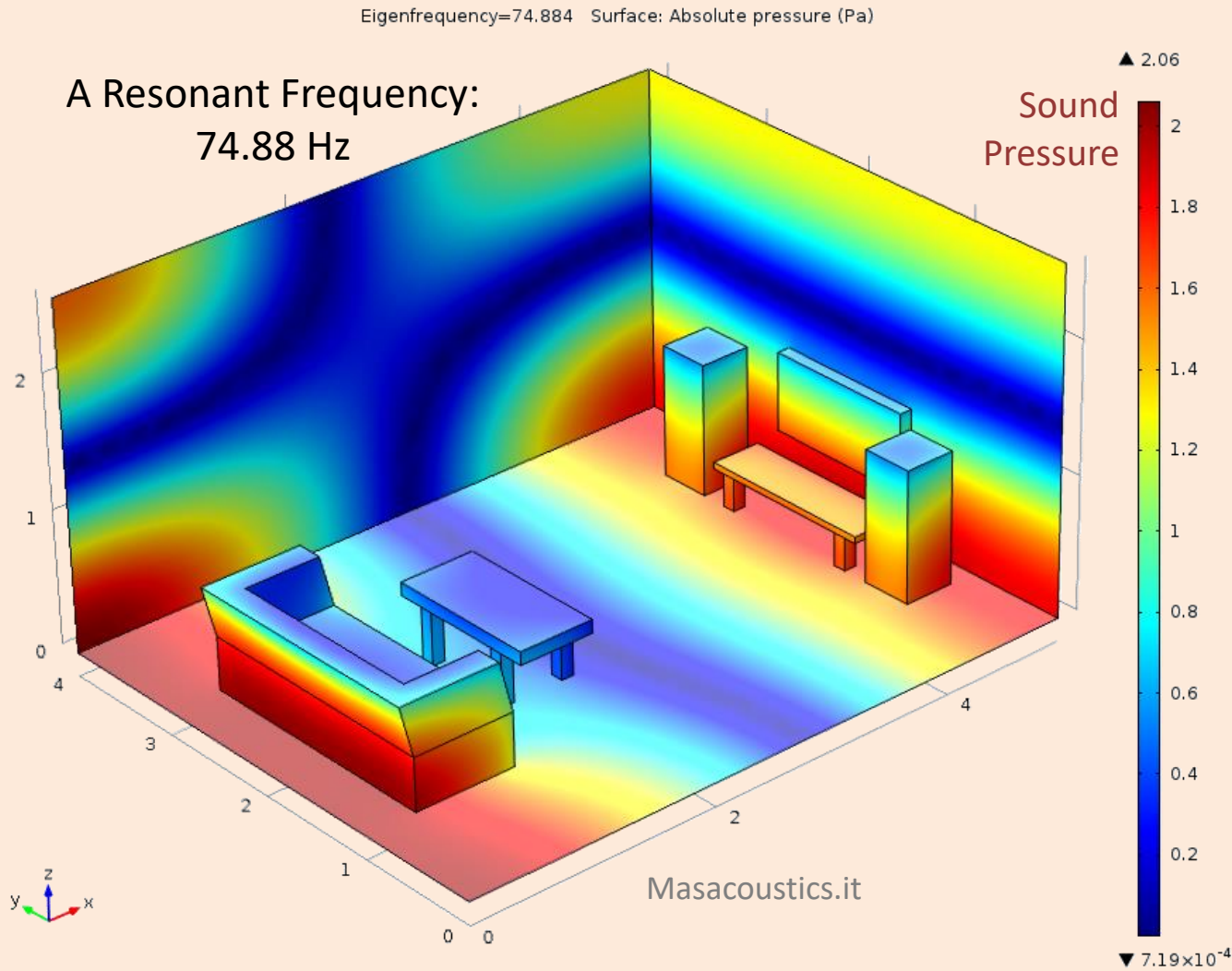
Groove from Led Zeppelin's "Good Times, Bad Times" (from the album "Led Zeppelin II").  
Drumeo  
YouTube ~2021

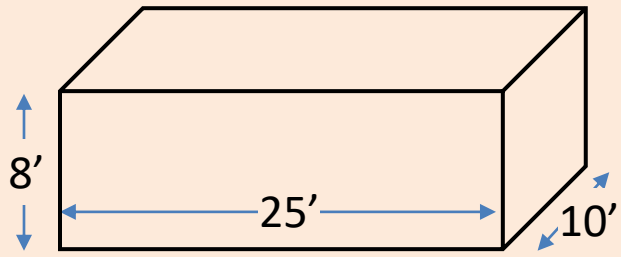
0 Hz



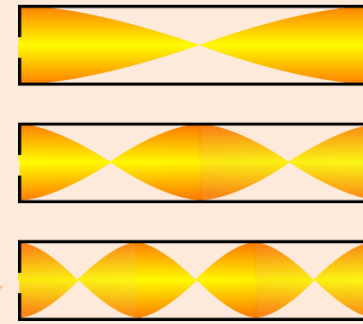


# Room Modes

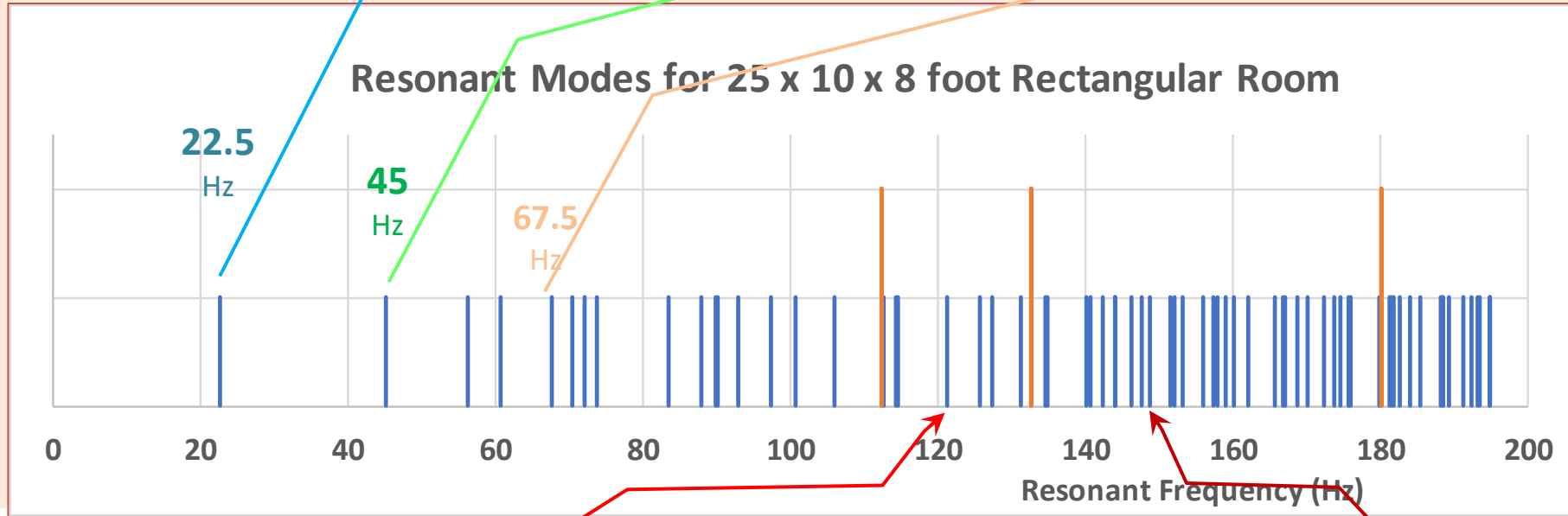




# Room Modes

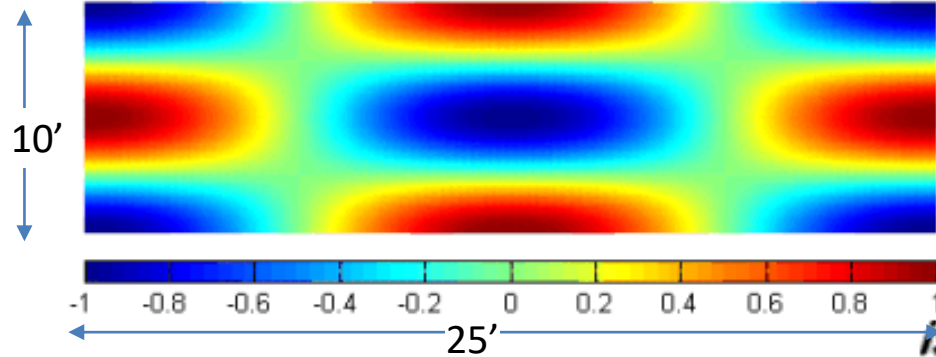


Longitudinal  
"Organ Pipe"  
modes

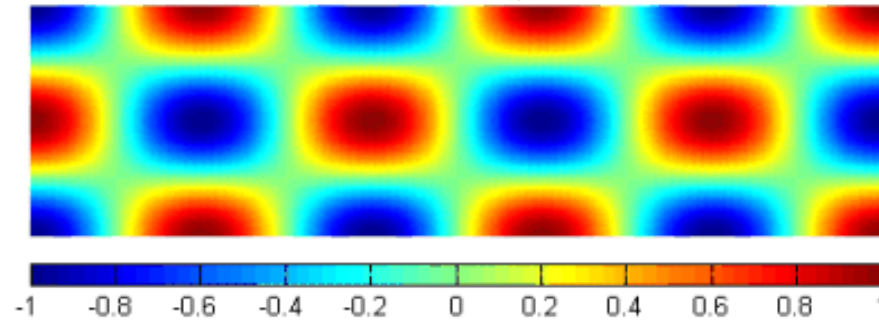


Pressure Mode

Pressure Mode



isvr



isvr

## Question Time

- Pipe Instruments
- Non-harmonic resonators
- Drums
- Room Resonances



# Course Outline



1. Building Blocks: Some basic concepts
- 2. Resonance: Building Complex Sounds**
3. Hearing and the Ear
4. Musical Scales and Musical Notation
5. Musical Instruments: Strings and Others
6. Musical Instruments: Pipes
7. Human Voice and Singing
8. Harmony and Dissonance; Chords